

# CBCS SCHEME

USN

--	--	--	--	--	--	--	--	--	--

18EE33

## Third Semester B.E. Degree Examination, Jan./Feb. 2021 Transformers and Generators

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

### Module-1

- 1
- Explain practical transformer on no-load. (04 Marks)
  - With the help of a neat circuit diagram and phasor diagram Explain the operation of a 3-phase star-Delta transformer. (06 Marks)
  - Draw the phasor diagram of a transformer supplying Lagging power factor load. (04 Marks)
  - A 230/460V single phase transformer has a primary resistance of 0.2 ohm and a reactance of 0.5ohm and the corresponding values for the secondary are 0.75 ohm and 1.8 ohm respectively. Find the secondary terminal voltage when supplying 10A at 0.8 power factor lagging. (06 Marks)

OR

- 2
- With neat circuit diagrams, discuss in detail how to perform OC and SC tests on single phase transformer. (08 Marks)
  - Explain with circuit diagram and phasor diagram how two transformers connected in open delta can supply the power successfully. (06 Marks)
  - Find the all day efficiency of a transformer having maximum efficiency of 98% at 15kVA at unity power factor and loaded as follows :  
12Hr 2kW at 0.5 power factor  
6 Hr 12kW at 0.8 power factor  
6 Hr No load. (06 Marks)

### Module-2

- 3
- With a neat circuit, explain how iron losses can be separated into hysteresis and eddy current losses in a transformer. (08 Marks)
  - List the conditions to be satisfied for parallel operation of single phase and Three phase transformers. (04 Marks)
  - Two 250kVA transformers supplying a network are connected in parallel on both primary and secondary sides. Their voltage ratios are same. The resistance drops are 1.5% and 0.9% and reactance drops are 3.33% and 4% respectively. Calculate the KVA loading on each transformer and its power factor. When the total load on the transformers is 500KVA at 0.707 lagging power factor. (08 Marks)

OR

- 4
- Obtain the expression for current shared by two transformers with unequal voltage ratios connected in parallel. The transformers have unequal internal impedance. Also draw the phasor diagram. (08 Marks)
  - In a 400V, 50Hz transformer, the total iron loss is 2500W. When the supply voltage and frequency reduced to 200V, 25Hz respectively the corresponding loss is 850W. Calculate the eddy current loss at normal voltage and frequency. (06 Marks)
  - An auto transformer supplies a load of 3kW at 115V, unity power factor. If the applied voltage is 230V, calculate the power transferred to the load i) inductively ii) conductively. (06 Marks)

Module-3

- 5 a. What is Cooling of transformer? List different methods of cooling and explain any two of them. (06 Marks)
- b. An 8 pole wave wound DC generator has 480 armature conductors. The armature current is 200A. Find the armature reaction demagnetizing and cross magnetizing ampere turns per pole, if the brushes are shifted  $6^\circ$  electrical from Geometrical natural axis. (06 Marks)
- c. Define: i) Distribution factor ii) Pitch factor. Derive the expressions for the factors. (08 Marks)

OR

- 6 a. Define Armature reaction in a DC generator. What are the effects of armature reaction? Explain. (06 Marks)
- b. With necessary diagrams, explain armature reaction in alternator for lagging, unity and leading power factors. (06 Marks)
- c. A 3 phase, 8 pole, star connected alternator has the armature coils short chording by 1 slot. The coil span is  $165^\circ$  electrical. The alternator is driven at the speed of 750rpm. If there are 12 conductors per slot, and flux per pole is 50mwb, calculate the value of the induced emf across the terminals. (08 Marks)

Module-4

- 7 a. Define voltage regulation of the alternator and explain the Ampere turn method of predetermination of regulation. (08 Marks)
- b. Define Short Circuit Ratio (SCR). Explain its significance. (04 Marks)
- c. A 3 phase 2000KVA star connected 50Hz, 2300V alternator has a resistance between each pair of terminals as measured by direct current is 0.16ohm. The alternator gave a short circuit current of 600A for a excitation. With same excitation the open circuit voltage is 900V (line). Determine the full load regulation at i) unity power factor ii) 0.8pf lagging. (08 Marks)

OR

- 8 a. Explain the zero power factor method of predetermination of regulation of an alternator. (08 Marks)
- b. Compare synchronous Impedance method and Ampere turn method of predetermining of regulation. (04 Marks)
- c. A 3.5MVA, star connected alternator, at 4160V at 50Hz has an open circuit characteristics as given by the following data :

$I_f$ , Amp	50	100	150	200	250	300	350
$V_{oc}$ , Volts (Line)	1629	3150	4160	4750	5130	5370	5550

A field current of 200A is found necessary to circulate full load current on short circuit. Calculate by Ampere turn method full load voltage regulation at 0.8pf lagging. (08 Marks)

Module-5

- 9 a. What is synchronization? Explain with the help of a neat sketch. The three lamps dark method of synchronization. (08 Marks)
- b. Derive an expression for the power angle characteristics of cylindrical rotor alternator. Sketch the power angle curve. (06 Marks)
- c. An alternator has a direct axis synchronous reactance of 0.7pu and a quadrature axis synchronous reactance of 0.4pu. It is used to supply full load at rated voltage at 0.8pf. Find the induced emf on open circuit. (06 Marks)

OR

- 10 a. With the help of a circuit diagram, explain the measurement of direct axis and quadrature axis reactances by slip test. (08 Marks)
- b. Draw and explain the capability curve of synchronous generator. (06 Marks)
- c. What is hunting in synchronous machines? How do you eliminate hunting? (06 Marks)

# TRANSFORMERS AND GENERATORS

18EE33

3<sup>rd</sup> SEM

SOLUTION FOR VTU QUESTION PAPER

JAN-FEB 2021

Prof: S.M. INAMADAR

## Module-1

1  
a Explain Practical Transformer on no load. [4 marks]

Soln: Practical Transformer on No load means secondary is not having any load.

Primary current under no load condition has to supply iron losses [hysteresis and eddy current loss] and primary copper loss.

$I_0$  = No load current = [3 to 5% of Full load current]

$I_{0m}$  = Magnetising component of No load current  
= Purely reactive and wattless component

$I_c$  = Power component of No load current  $I_0$   
= Active component and wattful component  
= Core loss component of No load current  $I_0$

$$I_0^{\wedge} = I_{0m}^{\wedge} + I_c^{\wedge}$$

$I_0$  lags  $V_1$  by angle  $\phi_0$

So  $\cos\phi_0$  = no load power factor

$W_0$  = Total power input on no load =  $V_1 \cos\phi_0 I_0$

$$W_0 = V_1 I_c \quad \because I_c = I_0 \cos\phi_0$$

$$W_0 = V_1 \cos\phi_0 I_0 = P_i = \text{Iron loss}$$

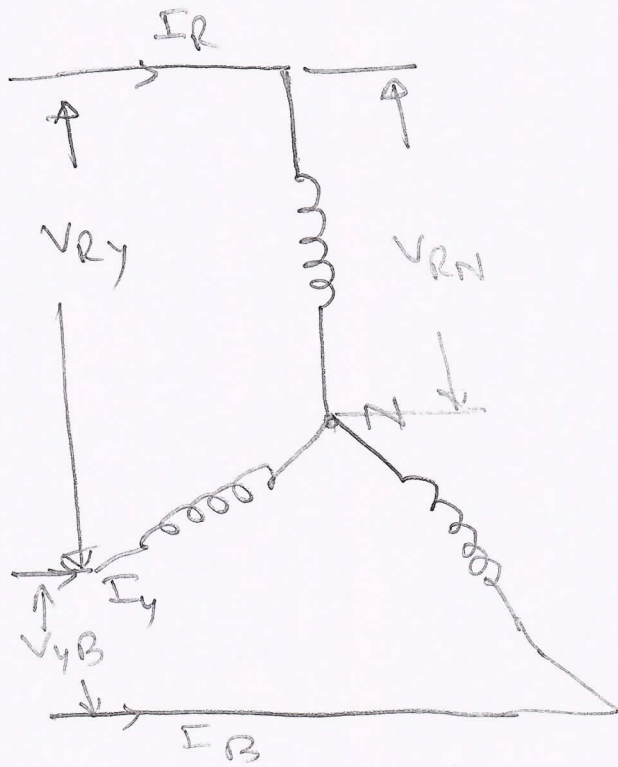
To minimize losses

High grade silicon steel is used

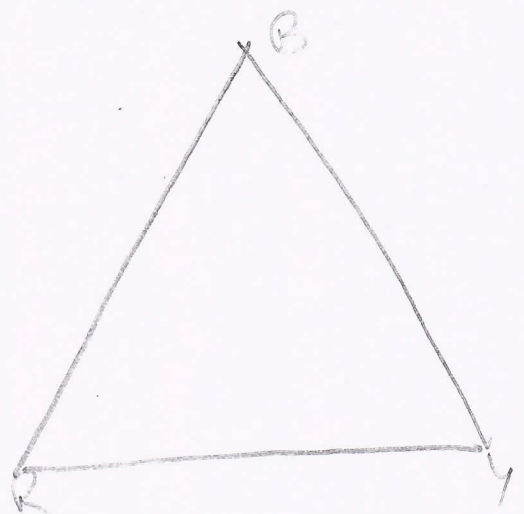
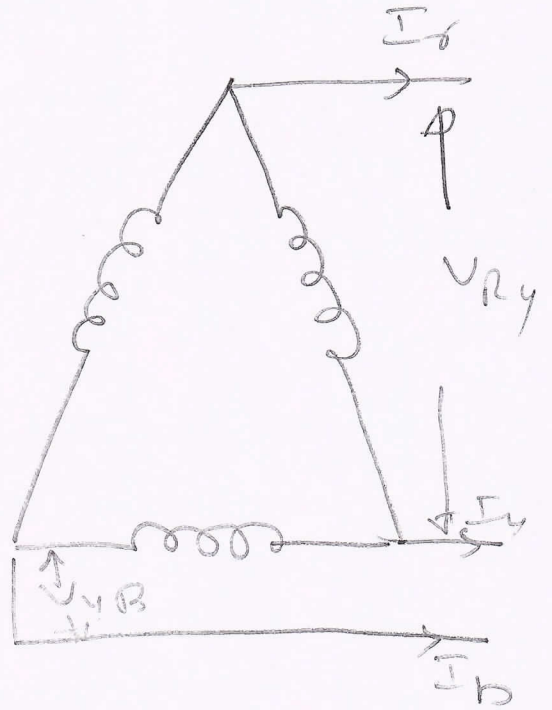
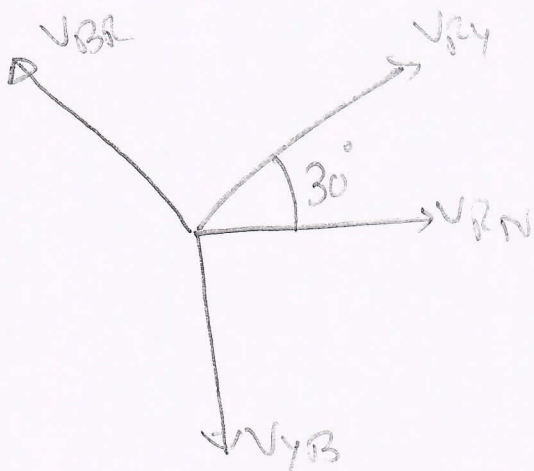
Laminated core are used to reduce eddy

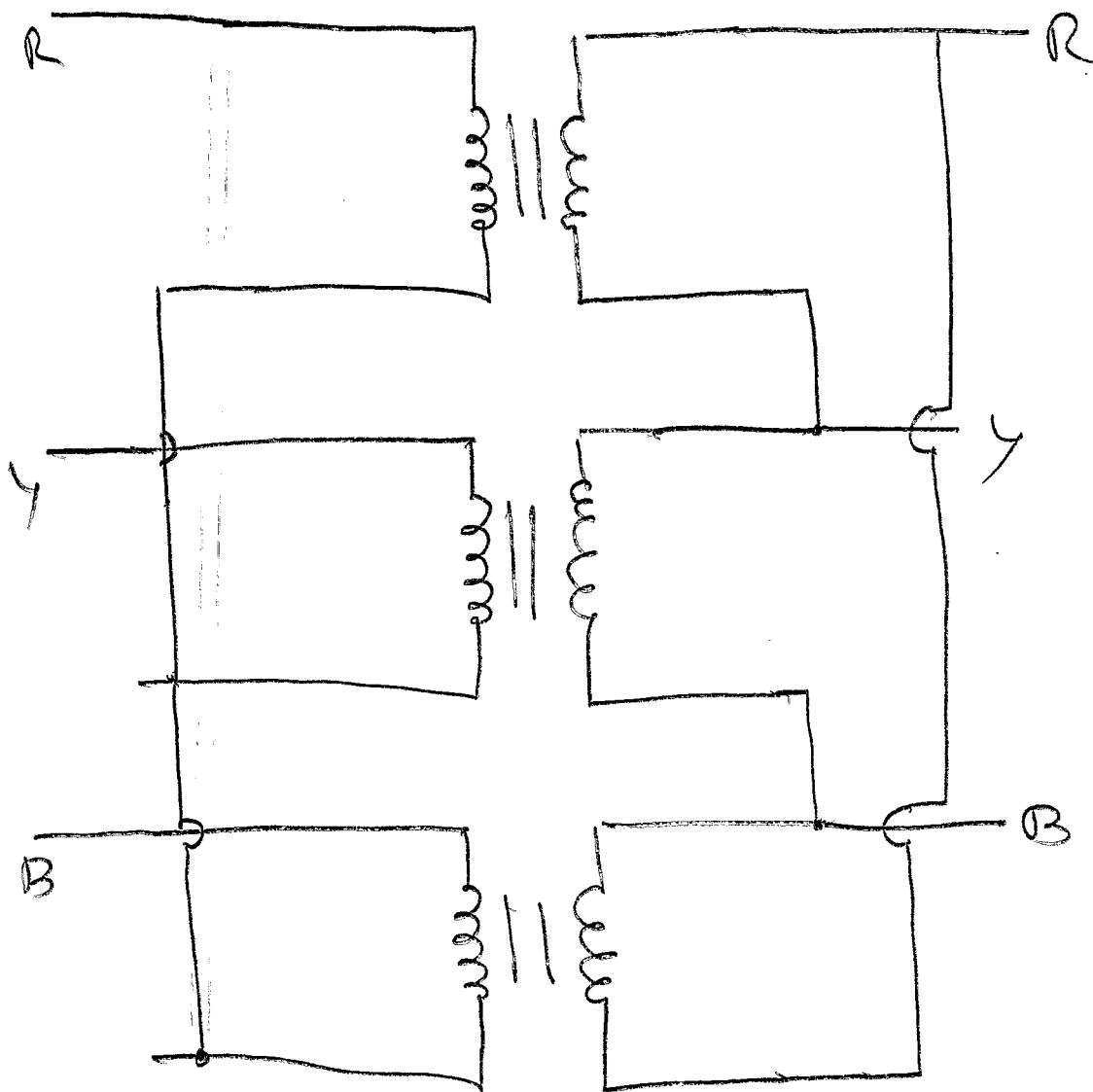
current loss.  $\eta = \frac{P_{out}}{P_{out} + P_i + P_{cu}}$

1 (b) With help of neat Circuit Diagram, Explain the operation of 3 phase star-delta Transformer (06 marks)



Primary side  
Vector Diagram





Equations for star

$V_{ph} = V_L / \sqrt{3} \Rightarrow$  Less no of turns, stress on insulation is less

$I_{ph} = I_{line} \Rightarrow$  windings can bear heavy load and short circuits.

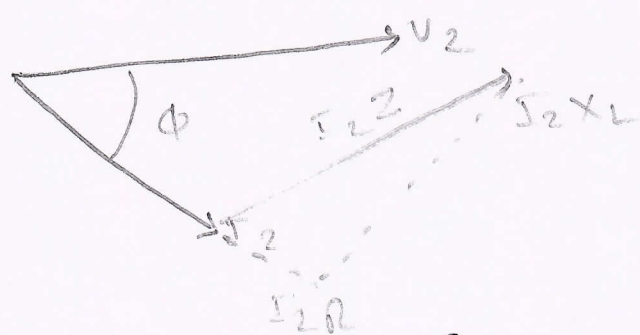
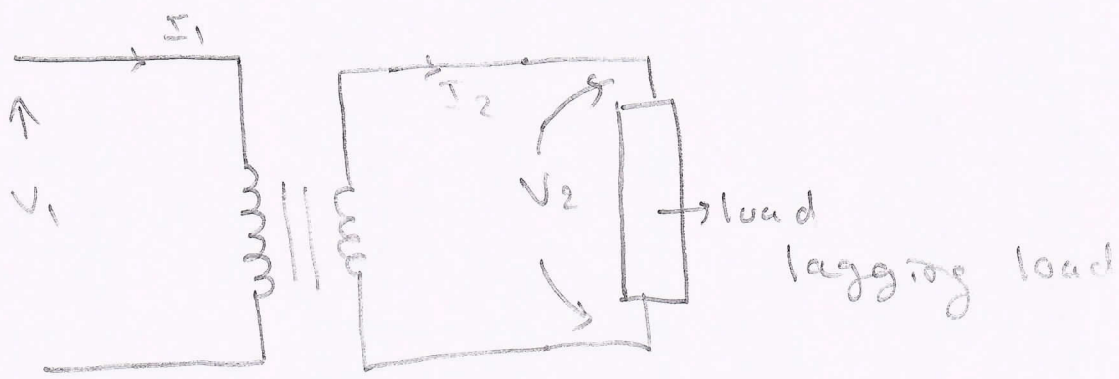
Equations for delta

$V_L = V_{ph}$   
 $I_{ph} = I_L / \sqrt{3} \Rightarrow$  Used for shedding of voltage

Star to delta connection involves phase difference of  $30^\circ$  between  $30^\circ$  from primary and secondary line voltage.

1  
c Draw the Phasor Diagram of Transformer supplying lagging power factor load. [04 marks]

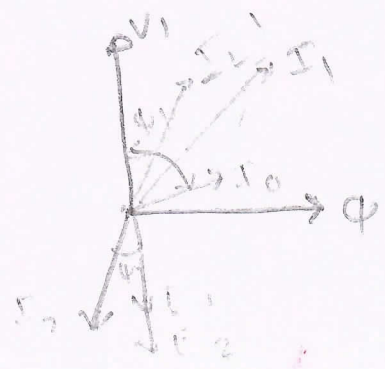
Soln:



$$\cos \phi = \text{Power factor} = \frac{R}{Z} = \frac{KW}{KVA}$$

$$\text{Load } Z = R + jX_L \quad \therefore \text{lagging load}$$

Circuit diagram and phasor diagram are drawn for lagging load.  $V_2$  is output of Transformer



1  
d A 230/460V, Single phase Transformer has a primary resistance of  $0.2 \Omega$  and reactance of  $0.5 \Omega$ , and corresponding values for secondary are  $0.75 \Omega$  and  $1.8 \Omega$  respectively. Find the secondary Terminal voltage when Supplying 10A at 0.8 p.f lagging. [06 marks]

Soln

$$230V / 460V$$

$$R_p = 0.2 \Omega \quad X_p = 0.5 \Omega$$

$$R_s = 0.75 \Omega \quad X_s = 1.8 \Omega$$

$$N_s = ? \quad I_L = 10A \quad \cos\phi = 0.8$$

lagging

$$\frac{V_2}{V_1} = \frac{460}{230} = k = 2 = \frac{I_1}{I_2}$$

$$I_{FL} = 10A$$

$$\begin{aligned} R_{equivalent} &= R_p + R_s' = R_p + \frac{R_s}{k^2} \\ &= 0.2 + \frac{0.75}{4} = 0.3875 \Omega \end{aligned}$$

$$X_{equivalent} = 0.2 + \frac{1.8}{4} = 0.65 \Omega$$

$$\cos\phi = 0.8 \quad \sin\phi = 0.6$$

$$\begin{aligned} \%R &= I_1 \left[ \frac{R_{equi} (\cos\phi - X_{equivalent} \sin\phi)}{V_1} \right] \times 100 \\ &= 10 \left[ \frac{0.3875 \times 0.8 - 0.65 \times 0.6}{230} \right] \times 100 \\ &= 0.043 \left[ 0.31 - 0.585 \right] \times 100 = -1.18\% \end{aligned}$$

(5)



$$\% \text{ Regulation} = \frac{E_2 - V_2}{E_2} \times 100$$

$$-1.18 = \left( \frac{460 - V_2}{460} \right) \times 100$$

$$-1.18 \times 460 = 460 - V_2$$

$$460 - V_2 = -1.18 \times 460$$

$$460 + 1.18 \times 460 = V_2$$

$$460 + 542.8 = V_2$$

$$V_2 = 542.8 \text{ V}$$

2  
(a)

With neat Circuit Diagrams, discuss in detail how to perform OC and SC tests on Single phase Transformer. [08 marks]

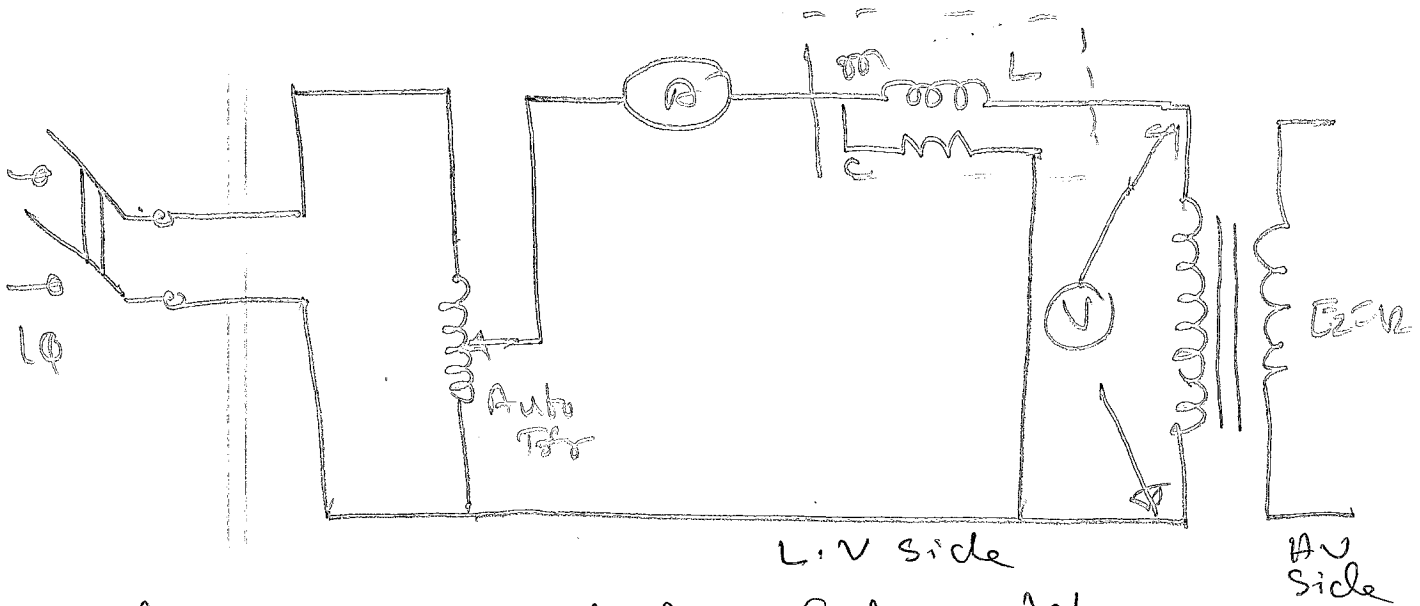
Soln:

Open circuit test is indirect loading method. Secondary is kept open of single phase transformer.

Primary side voltage of transformer is varied from zero volts to applied voltage by Auto transformer connected in primary. Wattmeter and ammeter connected gives the no load power and no load current of single phase transformer.

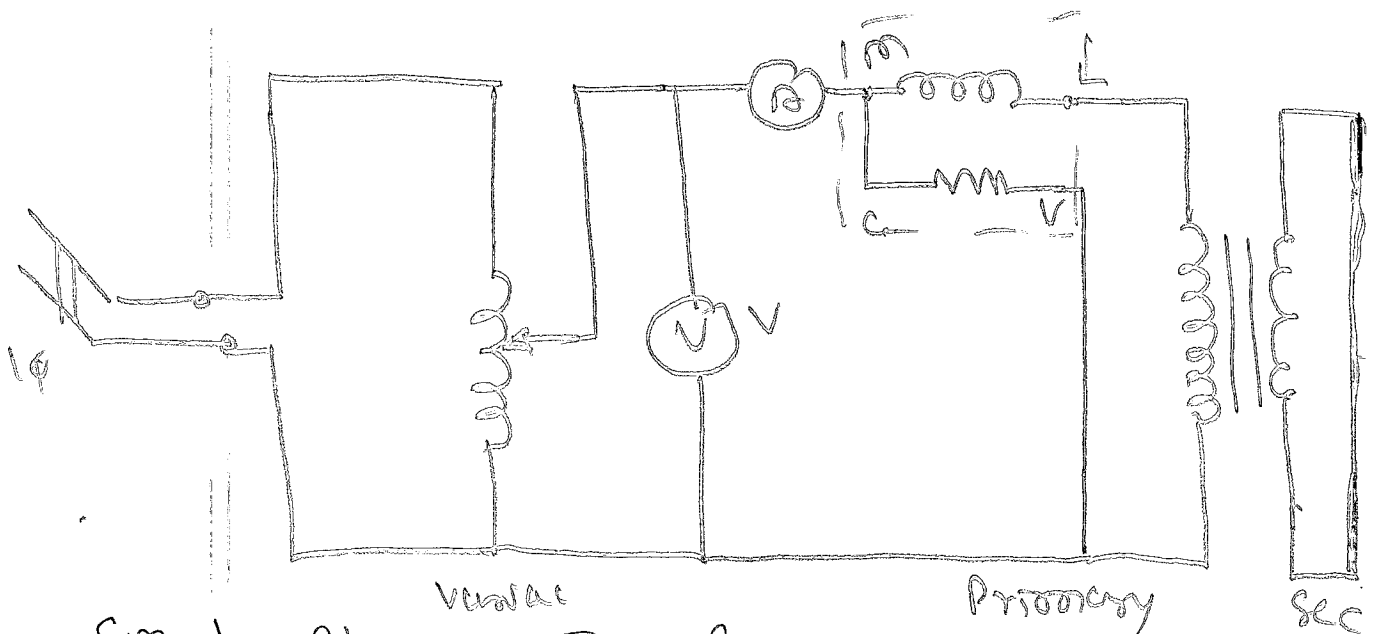
(6)

$V_0 =$  Rated voltage       $W_0 =$  Iron loss power  
 $I_0 =$  No load current



$\cos \phi_0 =$  No load power factor  $= \frac{W_0}{V_0 I_0}$   
 No load test gives info about iron losses which is constant for all loads

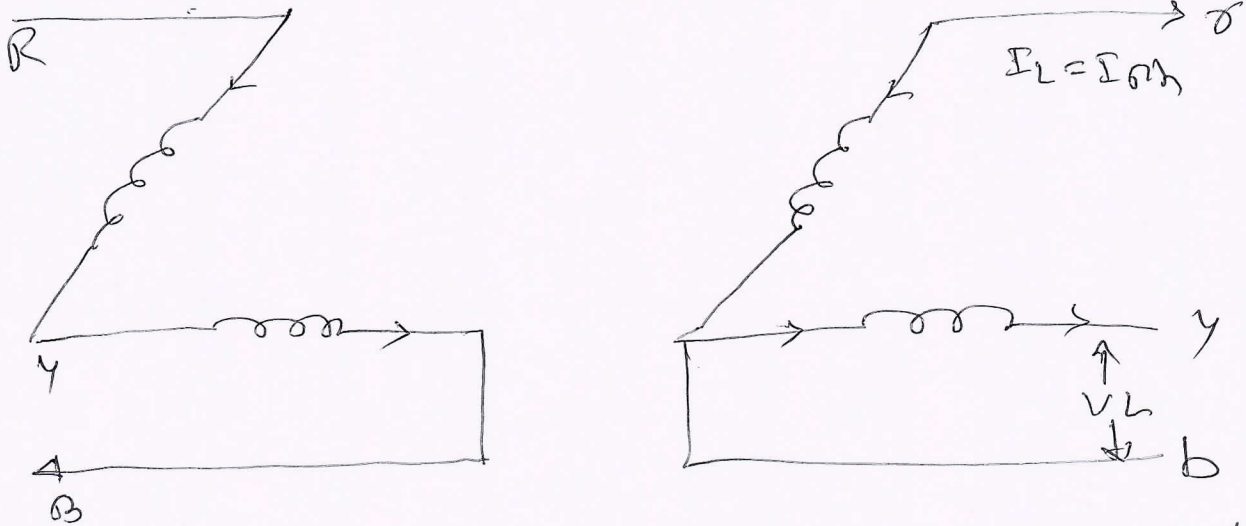
### Short Circuit Test



Single Phase Transformers secondary is shorted with thick wire of copper. Low voltage is applied at primary till rated current at primary is obtained.  
 $W_{sc} =$  Full load copper loss  $= I_{sc}^2 R_{sc} \cos \phi_{sc}$   
 $\cos \phi_{sc} =$  Short circuit power factor

2b Explain with Circuit Diagram and phasor diagram how two Transformers connected in Open Delta can supply power successfully [06 marks]

Soln:



Open Delta system helps to connect load in emergency if one transformer is under repair condition.

$$V-V \text{ Capacity} = \sqrt{3} V_L I_L$$

$$= \sqrt{3} V_L I_0 h$$

Comparing with D-D

$$D-D \text{ Capacity} = 3 V_L I_0 h$$

$$\frac{V-V \text{ Capacity}}{D-D} = \frac{\sqrt{3} V_L I_0 h}{3 V_L I_0 h} = \frac{1}{\sqrt{3}} = 58\%$$

we connect only 58% of load under V-V connection.

$$\text{Utility Factor} = \frac{\text{Operating Capacity in V-V}}{\text{Available Capacity in V-V}}$$

$$= 0.866$$

2c Find the All Day Efficiency of a Transformer having maximum efficiency of 98% at 15 kVA at unity power factor and loaded as follows.

- 1) 12 Hrs 2 kW at 0.5 power factor
- 2) 6 Hrs 12 kW at 0.8 power factor
- 3) 6 Hrs No load.

[06 marks]

Soln

Given Data

$$\eta = 98\%$$

$$kVA = 15 \text{ kVA at u.p.f}$$

$$\cos\phi = 1$$

$$\eta = \frac{[VA] \cos\phi}{[VA] \cos\phi + 2P_i} \times 100$$

$$0.98 = \frac{15 \times 1000 \times 1}{15 \times 1000 + 2P_i} \quad P_i = 153.061 \text{ W}$$

$$P_{cu} = P_i = 153.061 \text{ W}$$

$$\begin{aligned} \text{Energy output} &= 2 \text{ kW} \times 12 + 12 \text{ kW} \times 6 \\ &= 24 + 72 = 96 \text{ kWh} \end{aligned}$$

$$\begin{aligned} \text{Energy spent due to iron loss} &= P_i \times 24 \text{ Hrs} \\ &= 3.673 \text{ kWh} \end{aligned}$$

$$\cos\phi = \frac{kW}{kVA}$$

$$kVA = \frac{2}{0.5} = 4 \text{ kVA} \quad \text{From load 1}$$

$$kVA = \frac{12}{0.8} = 15 \text{ kVA} \quad \text{From load 2}$$

$$\begin{aligned} \text{load 1 } P_{cu} &= P_{cu} \text{ at } 15 \text{ km/h} \left(\frac{4}{15}\right)^2 \\ &= 153.061 \times 0.07111 \\ &= 10.8843 \text{ W} \end{aligned}$$

$$\begin{aligned} \text{Energy Spent} &= \text{load 1 } P_{cu} \times \text{time} \\ &= 10.8843 \times 12 \\ &= 130.6116 \text{ Wh} \\ &= 0.130 \text{ kWh} \end{aligned}$$

$$\begin{aligned} \text{load 2 } P_{cu} &= P_{cu} \text{ at } 15 \text{ km/h} \\ &= 153.061 \text{ W} \end{aligned}$$

$$\begin{aligned} \therefore \text{Energy Spent} &= 153.061 \text{ W} \times 6 \\ &= 918.366 \\ &= 0.9183 \text{ kWh} \end{aligned}$$

$$\begin{aligned} \therefore \text{Total Energy Spent} &= 0.130 + 0.9183 + 3.6734 \\ &= 4.7226 \text{ kWh} \end{aligned}$$

$$\text{All Day Efficiency} = \frac{\text{Total Energy Output in 24 hr}}{\text{Total Energy Input in 24 hr} + \text{Energy Spent in 24 hr}}$$

$$\begin{aligned} &= \left[ \frac{96}{96 + 4.7236} \right] \times 100 \\ &= 95.31\% \end{aligned}$$

All Day efficiency is 95.31%

## Module - 2

3 (a) With a neat circuit, Explain how iron losses can be separated into hysteresis and Eddy Current losses in transformers. [08 marks]

Soln:

$$\begin{aligned} \text{Core losses} &= \text{hysteresis losses} + \text{Eddy losses} \\ &= P_h + P_e \\ &= k_h B_{\text{max}}^{1.62} f v + k_e B_{\text{max}}^2 f^2 \end{aligned}$$

$$\begin{aligned} P_i &= P_h + P_e \\ &= A B_{\text{max}}^{1.62} f + B B_{\text{max}}^2 f^2 \end{aligned}$$

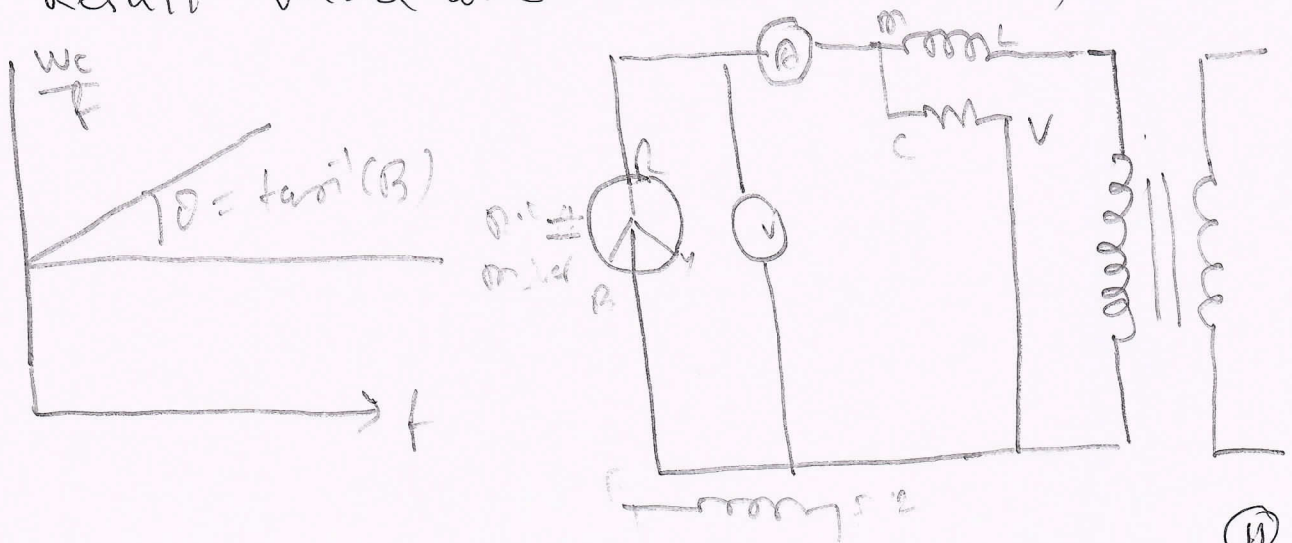
Test 1  $\Rightarrow$  at  $P_1$  frequency

Test 2  $\Rightarrow$  at  $P_2$  frequency

$$B_{\text{max}} = \text{Test 1} = \text{Test 2}$$

$I_0$ ,  $W_0$ ,  $\cos \phi_0$  are calculated

Result values are used to identify A, B



3

b

List the Conditions to be satisfied for parallel operation of single phase and 3 phase Transformers. [04 marks]

Soln:

Conditions for Single Phase parallel operation

- 1) Transformers connected have same polarity
- 2) Voltage ratios of primary and secondary of Transformers must be same.
- 3) Percentage impedance should be equal in magnitude, to avoid circulating currents.
- 4) If Transformers have different KVA rating, then equivalent impedance should be inversely proportional to individual KVA ratings

Condition for Three phase parallel operation

- 1) Angular Displacements and phase rotation between two units to be made parallel, must be same.
- 2) Standard lead marks are used for connecting in parallel.
- 3) Ratio of  $(R/X)$  must be same for both transformers.
- 4) Voltage ratios must be same.
- 5) Ratio of Equivalent  $X_L$  to Equivalent  $R$  should be same.

3  
c Two 250 kVA Transformers supplying a network are connected in parallel on both primary and secondary side. Voltage ratios are same. Resistance drops are 1.5% and 0.9% and reactance drops are 3.33% and 4%. Calculate kVA loading on each Transformer and its power factor. When the total load on Transformer is 500 kVA at 0.707 lagging power factor. [08 marks]

Soln: (Q1) Transformer 1  $\Rightarrow z_1 = R_1 + jX_1 = 1.5 + j3.33$   
 $\Rightarrow z_1 = 1.5 + j3.33 = 3.65 \angle 65.75^\circ$

(Q2) Transformer 2  $\Rightarrow z_2 = R_2 + jX_2$   
 $= 0.9 + j4 = 4.1 \angle 77.32^\circ$

$Q = 500 \text{ kVA}$   $\cos \phi = 0.707$   $\phi = 45.0^\circ$

$z_1 + z_2 = 1.5 + j3.33 + 0.9 + j4$   
 $= 2.4 + j7.33 = 7.713 \angle 71.87^\circ$

$Q_1 = Q \left[ \frac{z_2}{z_1 + z_2} \right] = 500 \angle -45.0^\circ \left[ \frac{4.1 \angle 77.32^\circ}{7.713 \angle 71.87^\circ} \right]$

$Q_1 = 265.78 \angle -39.55^\circ$

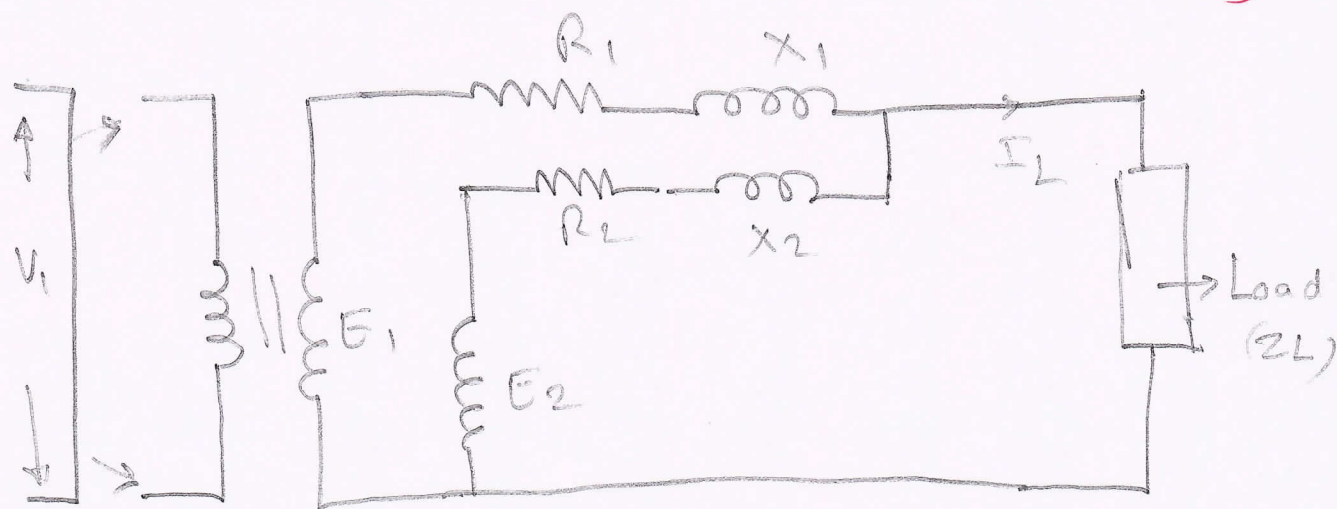
$Q_2 = 500 \angle -45.0^\circ \left[ \frac{z_1}{z_1 + z_2} \right] = \frac{3.65 \angle 65.75^\circ}{7.713 \angle 71.87^\circ}$

$Q_2 = 236.009 \angle -50^\circ$   
 kVA load shared is 265 and 236



4

(a) Obtain the Expression for Current Shared by two transformers with unequal voltage ratios connected in parallel. The transformers have unequal internal impedance. Also draw the phasor diagram. [08 marks]



Let voltage ratio of Transformer 1 is more than 2nd Transformer.

$$\text{So } E_1 > E_2$$

$$\text{Terminal voltage} \approx (E_1 - E_2)$$

$$I_c = \text{Circulating Current} = \frac{E_1 - E_2}{Z_1 + Z_2}$$

$$E_1 = V_2 + I_1 Z_1 \quad E_2 = V_2 + I_2 Z_2$$

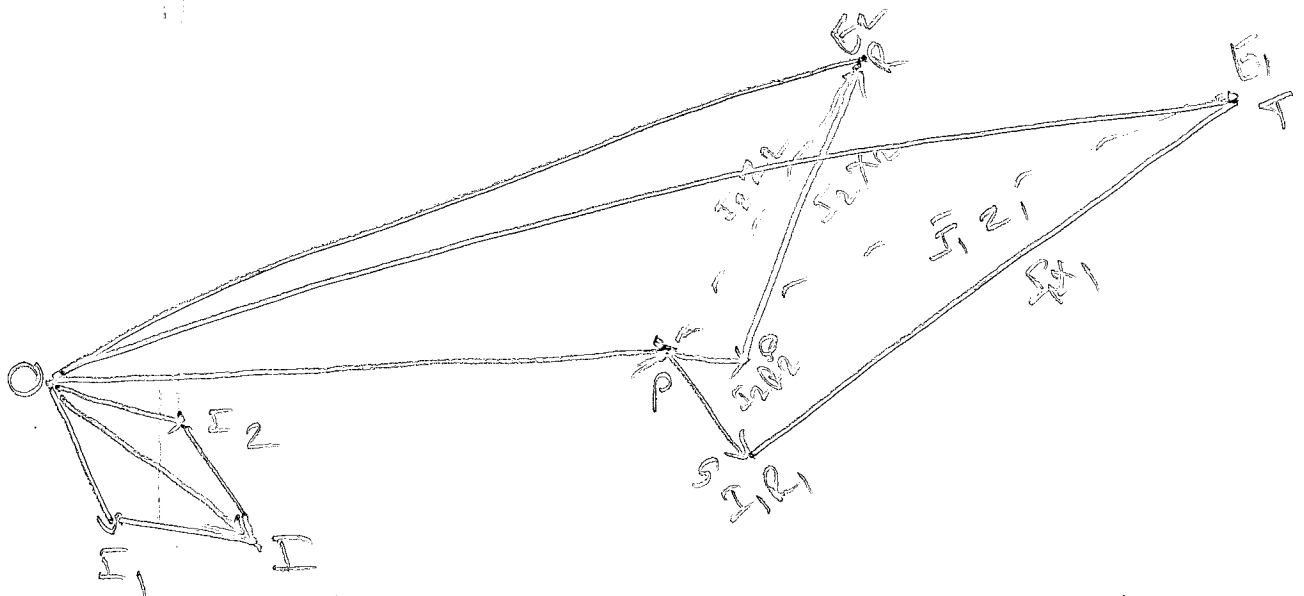
$$\text{Let } I_L = I_1 + I_2$$

$$I_1 = \frac{(E_1 - E_2) + I_2 Z_2}{Z_1}$$

$$I_2 = \frac{E_2 Z_1 - (E_1 - E_2) Z_L}{Z_1 Z_2 + Z_L (Z_1 + Z_2)}$$

$$I_1 + I_2 = \frac{E_1 Z_2 + E_2 Z_1}{Z_1 Z_2 + Z_L (Z_1 + Z_2)}$$

Phasor Diagram



$$V_2 = \frac{E_1}{Z_1} + \frac{E_2}{Z_2} \bigg/ \frac{1}{Z_L} + \frac{1}{Z_2} + \frac{1}{Z_1}$$

4  
(b)

In a 400V, 50 Hz Transformer, total iron loss is 2500 W. When supply voltage and frequency reduced to 200V, 25 Hz respectively, corresponding loss is 850 W. Calculate the eddy current loss at normal voltage and frequency. [06 marks]

Soln:

$$\text{Total iron loss} = 2500 \text{ W}$$

$$P_i = P_h + P_e = Af + Bf^2$$

$$2500 = A \times 50 + B(50)^2$$

$$850 = A \times (25) + B(25)^2$$

$$\frac{2500}{850} = \frac{(50A + 50^2 B)}{(25A + 25^2 B)}$$

$$2500(25A + 25 \times 25B) = 850(50A + 50 \times 50B)$$

$$62500A + 1562500B = 42500A + 2125000B$$

$$20000A = 562500B$$

$$A = \frac{562500B}{20000}$$

$$A = 28.125B$$

$$2500 = 28.125B \times 50 + 2500B$$

$$2500 = 3906.25B$$

$$B = 0.64 \quad A = 18$$

Eddy current loss at normal voltage and frequency

$$P_e = Bf^2 = 0.64 \times 50 \times 50 = 1600 \text{ W}$$

$$\boxed{P_e = 1600 \text{ W}}$$

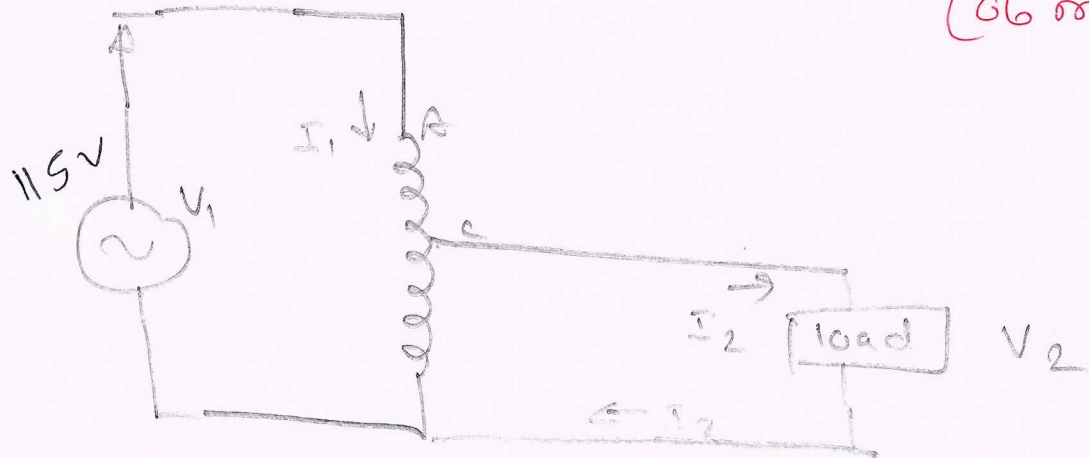
(16)

4  
C

An Auto Transformer supplies a load of 3 kW at 115 V, unity power factor. If voltage is 230 V, Calculate power transferred to load  
 i) Inductively ii) Conductively

(6 marks)

Soln:



115 V

$$\cos \phi = 1 = \cos \phi_2 \quad \text{load} = 3 \text{ kW}$$

230 V

$$P_{\text{out}} = V_2 I_2 \cos \phi_2$$

$$3 \text{ kW} = 115 \times I_2 \times 1$$

$$I_2 = 26.086 \text{ A}$$

Inductively let us assume  $\cos \phi_2 = 0.8$

$$P_{\text{out}} = V_2 I_2 \cos \phi_2$$

$$= 230 \times 26.086 \times 0.8$$

$$P_{\text{out}} = 4799 \text{ watts}$$

$$P_{\text{out}} = 4.8 \text{ kW}$$

Conductively load

$$P_{\text{out}} = V_2 I_2 \cos \phi_1$$

$$= 230 \text{ V} \times 26.086 \times (0.8)$$

$$P_{\text{out}} = 4.8 \text{ kW}$$

## Module - 3

5  
(a)

What is Cooling of Transformers? List different methods of cooling and explain any two of them. (06 marks)

Cooling of Transformer is the protection applied against the heat developed in transformer due to iron loss and copper loss. Coolant is external air or transformer oil or external fan.

List of different cooling methods

- 1) Air Natural (AN) Dry Type Transformer
- 2) Air Blast (AB) - Compressed Air, Blower, Fan
- 3) Oil Natural (ON) - oil Filled Transformer
- 4) Oil Natural Air Forced (ONAF) - "
- 5) Oil Natural Water Forced (ONWAF) - "
- Oil forced methods with Heat Exchanger
- 6) Oil Forced Air Natural (OFAAN)
- 7) Oil Forced Air Forced (OFAF)
- 8) Oil Forced Water Forced (OFWF)

Oil forced Air forced method uses heat exchanger. At higher loads, both fan & pump are switched on. Efficiency is high. Example is 1000VA transformer having conservator tank.

Oil forced water forced method uses heat exchanger and water inlet is provided more than 3000VA rating. This method is applied

5  
(b)

A 8 pole D.C. Generator has 480 armature conductors.  $I_a$  is 200 A. Find armature reaction demagnetizing and cross magnetizing ampere turns per pole, if the brushes are shifted  $6^\circ$  electrical from geometrical neutral axis. (06 marks)

Soln

$$P = 8 \quad Z = 480 \quad I_a = 200 \text{ A}$$

$$I = \frac{I_a}{2} = \frac{200}{2} = 100 \text{ A}$$

Since D.C. generator is wave wound

$$A = 2$$

Since brushes are shifted  $6^\circ$  electrical from GNA

$$\alpha_m = \frac{\alpha_e}{P/2} = \frac{6}{8/2} = \frac{6}{4} = 1.5^\circ$$

Demagnetizing AT are

$$AT_d / \text{pole} = Z I \frac{\alpha_m}{360} = \frac{480 \times 100 \times 1.5}{360}$$

$$\boxed{AT_d / \text{pole} = 200}$$

Cross magnetizing  $AT_c / \text{pole}$

$$AT_c / \text{pole} = Z I \left[ \frac{1}{2P} - \frac{\alpha_m}{360} \right]$$

$$= 480 \times 100 \left[ \frac{1}{16} - \frac{1.5}{360} \right]$$

$$\boxed{AT_c / \text{pole} = 2800}$$

5c Define  
 i) Distribution Factor ii) Pitch Factor  
 Derive Expression for the Factor.

(08 marks)

Soln) i) Distribution Factor (kd)

The factor by which there is reduction in the e.m.f. due to distribution of coils is called distribution factor (kd)

Derivation

let  $m =$  no of phase = ex: 3

$n =$  slots / pole

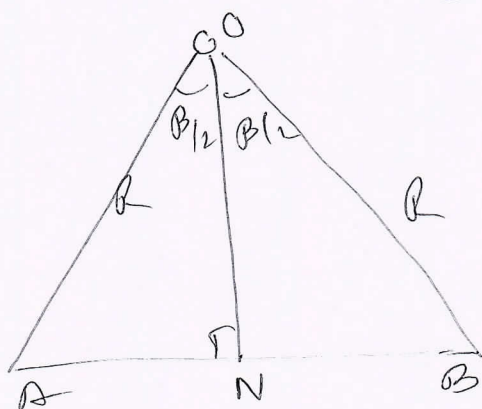
let  $F =$  no of coils under pole / phase

and in series.

$E =$  induced e.m.f / coil

let  $C =$  no of slots / pole / phase

$$\beta = \frac{180^\circ}{C}$$



$$E_R = \text{Resultant e.m.f.} \\ = CR$$

$$E = 2R \sin\left(\frac{\beta}{2}\right)$$

$$E_R = 2CR \sin\left(\frac{\beta}{2}\right)$$

$$k_d = \frac{E_R \text{ when coils are distributed}}{E_R \text{ when coils are connected}} \\ = \sin\left(\frac{C\beta}{2}\right)$$

$$* k_d = \frac{C \sin\left(\frac{\beta}{2}\right)}{\text{Always less than } (1)}$$

## ii) Pitch Factor

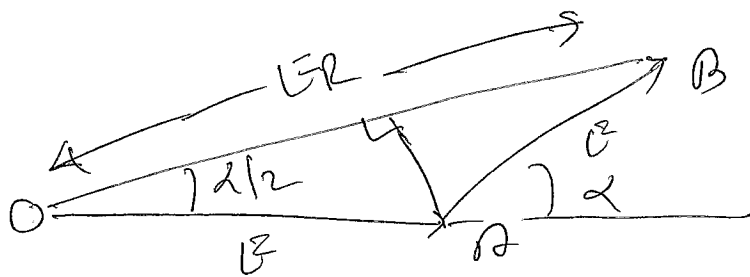
It is defined as ratio of resultant e.m.f. when coil is short pitched to the resultant e.m.f. when coil is full pitched.

$\alpha$  = Angle of short pitch

$\alpha$  =  $\beta \times$  No of slots by which coils are short pitched.

$\alpha$  =  $180^\circ$  - Actual coil span of coils.

$$k_c = \frac{E_R \text{ when coil (short pitched)}}{E_R \text{ when coil (is full pitched)}}$$



$$E_R = 2E \cos(\alpha/2)$$

When coils are short pitched, two e.m.f. in two coil sides are always in phase.

$$k_c = \frac{2E \cos(\alpha/2)}{2E}$$

Pitch Factor = Coil Span Factor



6  
(a) Define Armature Reaction in D.C. Generators.  
What are the effects of Armature Reaction?  
Explanation [06 marks]

Soln: Definition of Armature Reaction

The effect of Armature Flux provided by armature conductors on the distribution of main field flux [by field coil] is called Armature Reaction.

Effects of Armature Reaction

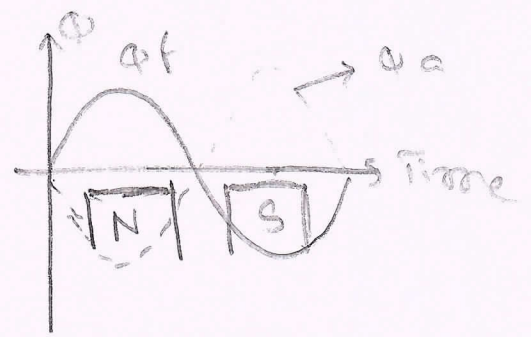
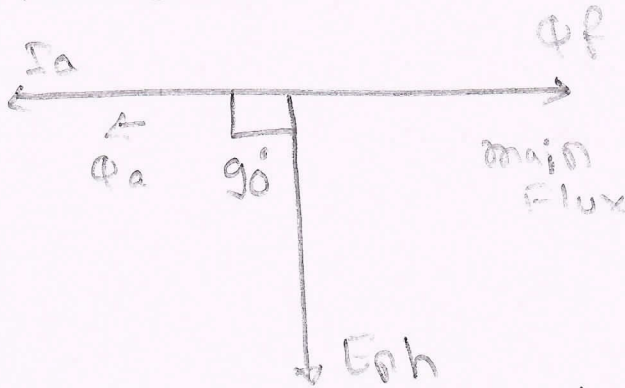
- 1) Generated EMF is reduced due to decrease in Flux/pole value.
- 2) Iron loss in teeth and pole shoe are more on load than without any load.
- 3) Comm. Increase, in turn  $V_{max}$  between adjacent commutator segments at load. If voltage exceeds 30V, then sparking occurs.
- 4) Brush Axis is shifted from GNA these will be induced e.m.f in coil undergoing commutation which will try to maintain current in original direction. So overall commutation is delayed.

The pole dip which is met first during rotation by armature conductors is known as leading pole dip and other is known as trailing pole dip.

6 (b) With necessary diagrams, Explain armature Reaction for lagging, unity and leading Power Factor for alternator (06 marks)

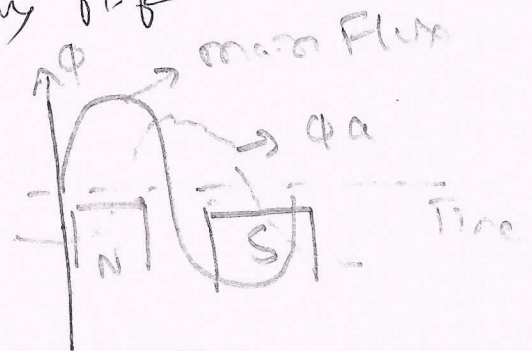
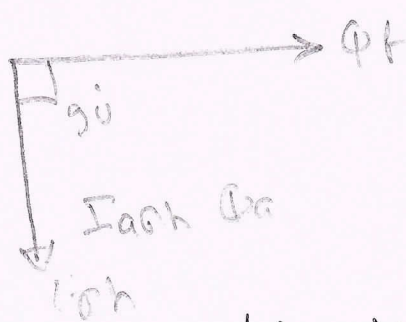
Soln

Armature Reaction for lagging P.F



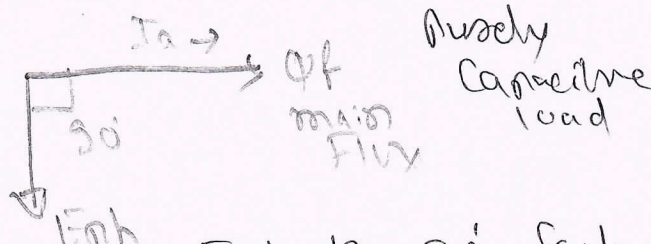
Purely inductive load  $I_{a\text{ph}}$  lags  $E_{\text{ph}}$  by  $90^\circ$   
 $\Phi_a$  is in same direction as that of  $I_a$ .  
 Armature Flux and main Flux are in opposite direction, we call it as Demagnetizing effect.

Armature Reaction for Unity P.F

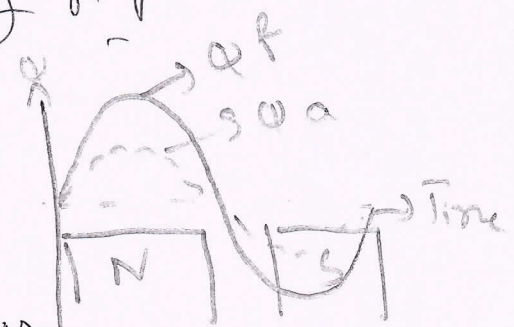


Purely resistive load, Average Flux in airgap remains constant but its distribution gets distorted, we call it as Cross magnetizing effect.

Armature Reaction for leading P.F



Purely Capacitive load

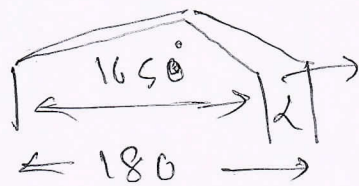


$E_{\text{ph}}$  leads  $I_{a\text{ph}}$  by  $90^\circ$ . Each Flux helps each other. Magnetizing effect.

6  
(C) A 3 $\phi$ , 8 pole star connected Alternator has armature coils short chorded by 1 slot. Coil span is  $165^\circ$  Electrical. Alternator is driven at speed of 750 r.p.m. If there are 12 conductors/slot, find Flux/pole is 50 mwb, Calculate value of induced e.m.f across the terminals [08 marks]

Soln:

$P = 8$       3 $\phi$ , 50 Hz, star connected  
 $N_s = 750$  r.p.m      Coil span =  $165^\circ$



chorded by 1 slot

$$\alpha = 180^\circ - 165^\circ = 15^\circ$$

$$\alpha = \beta = 15^\circ$$

$$\beta = \frac{180^\circ}{n} = \frac{180^\circ}{15^\circ} = 12 = \text{slots/pole}$$

1 slot = 12 conductors

slots/pole = 12

rotor pole = 8

$$\text{Total slots} = 8 \times 12 = 96$$

$$Z = \text{Total conductors} = 96 \times 12 = 1152$$

$$k_d = \frac{\sin \frac{n\beta}{2}}{n \sin \beta/2} = \frac{\sin \left( \frac{4 \times 15^\circ}{2} \right)}{4 \sin \left( \frac{15^\circ}{2} \right)} = 0.9526$$

$$k_c = \cos \frac{\alpha}{2} = \cos \left( \frac{15^\circ}{2} \right) = 0.9914$$

$$f = \frac{750 \times 8}{120} = 50 \text{ Hz}$$

$$T_{ph} = \frac{Z_{ph}}{2} = \frac{1152/8}{2} = 1152/6 = 192$$

$$E_{ph} = 4.44 k_c k_d \phi f T_{ph}$$

$$= 4.44 \times 0.9914 \times 0.9526 \times 50 \times 10^3 \times 50 \times 192$$

$$= 20023 \text{ kV}$$

$$E_{line} = \frac{20023}{\sqrt{3}} \times 2.023 = 3.501 \text{ kV}$$

(24)

## Module - 4

7 Define Voltage Regulation of Alternator and Explain Ampere Turn method of predetermination of regulation. [Cos medes]

Soln: Definition of Voltage Regulation  
: Voltage Regulation of Alternator is defined as the change in its terminal voltage when full load is removed, keeping field excitation and speed constant, divided by rated Terminal voltage.

$$\% \text{ Regulation} = \frac{E_{ph} - V_{ph}}{V_{ph}} \times 100$$

$E_{ph}$  = No load induced EMF

$V_{ph}$  = Rated Terminal voltage

It depends on Load currents and Power Factor. For lagging and unity p.f., there is drop in terminal voltage, hence regulation values are always +ve. For leading p.f., regulation is -ve.

Explanation for Ampere Turn Method

This method needs Results of Open Circuit Test and Short Circuit Test. It is also called Rother's m.m.f method.

magneto motive force (m.m.f) = Field current  $\times$  Turns

i) m.m.f necessary to induce rated Terminal voltage on open circuit.

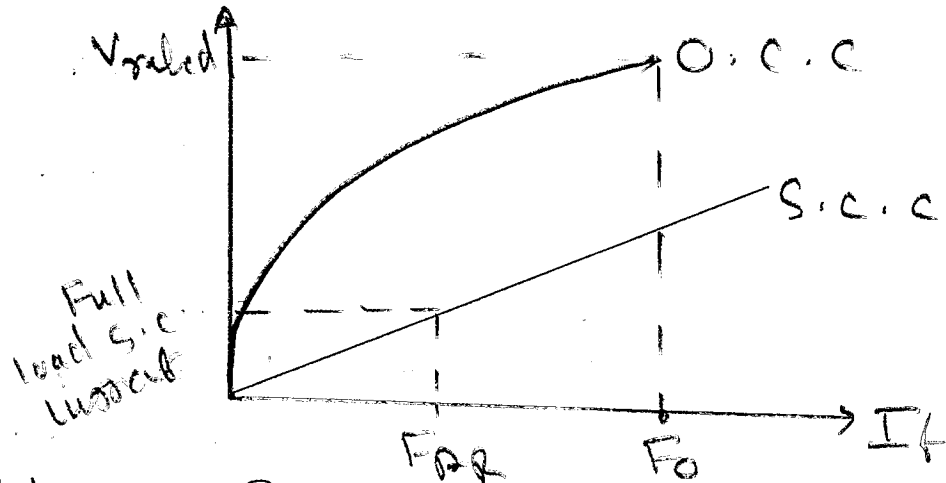
ii) m.m.f equal and opposite to that of Armature Reaction m.m.f.

$$Z_s = R_a + jX_s$$

$$X_s = X_L \text{ leakage} + X_L \text{ (Armature Reaction)}$$

In short circuit test,  $\cos \phi$  is necessary to overcome drop across  $R_a$  and  $X_L$  and to overcome effect of Armature reaction. Field  $\cos \phi$  is required to counterbalance armature reaction effect.

$F_{AR}$  = Armature Turns Required to Counterbalance  $I_{FL}$  from s.c test.



Field  $\cos \phi$  is used for overcoming Armature reaction which is demagnetising.

Total Field  $\cos \phi$  = vector sum of  $F_o$  and  $F_{AR}$

Zero lagging p.f (Demagnetising) =  $F_R = F_o + F_{AR}$

Zero leading p.f (magnetising) =  $F_R = F_o - F_{AR}$

unity p.f (non magnetising) =  $F_R = F_o^2 + F_{AR}^2$

$\cos \phi$  (lagging) =  $(F_R)^2 = (F_o + F_{AR} \sin \phi)^2 + (F_{AR} \cos \phi)^2$

$\cos \phi$  (leading) =  $(F_R)^2 = (F_o - F_{AR} \sin \phi)^2 + (F_{AR} \cos \phi)^2$

% Regulation =  $(V_{OH} - V_{OH}) / V_{OH} \times 100$   
Open circuit method (test value)

7 (b) Define Short Circuit Ratio (SCR)  
 Explain its Significance [08 marks]

Soln: Definition of Short Circuit Ratio  
 It is the ratio of excitation required to produce open circuit voltage equal to the rated voltage to the excitation required to produce rated full load current under short circuit.

$$S.C.R = \frac{I_f \text{ rated o.c. Voltage}}{I_f \text{ rated s.c. Current}}$$

$$Z_s = \frac{V_{oc} \text{ (phase)}}{I_a \text{ (s.c.) (phase)}} = X_s$$

Neglecting  $R_a$

$$X_s \text{ (pu)} = \frac{X_s / \text{Base Impedance}}{\text{Base Impedance}} = \frac{V_{\text{rated}} / \text{phase}}{I_a \text{ (rated)} / \text{phase}}$$

$$S.C.R = \frac{1}{X_s \text{ (per unit)}}$$

Significance

- 1) Low S.C.R  $\Rightarrow$   $X_s$  is high,  $(I_a X_s)$  is more  $\Rightarrow$  large changes in excitation for small changes in load.
- 2) Low S.C.R  $\Rightarrow$  Smaller Air Gap and poor voltage regulation.
- 3) Low S.C.R  $\Rightarrow$   $X_s$  is high synchronizing power decreases, stability decreases
- 4) By increasing air gap, S.C.R can be increased.

7  
(c)

A 3 phase 2000 kVA, star connected 50 Hz, 2300 V alternator has a resistance between each pair of terminals as measured by direct current is 0.16 Ω. (ohms). Alternator gave a short circuit current of 600 A for excitation. With same excitation the open circuit voltage is 900V (line)  
 Determine Full load Regulation at  
 i) Unity P.F ii) 0.8 P.F lagging

Soln:

Data given  
 2000 kVA, Star Connection, 2300 V

$$R_a = \frac{0.16}{2} = 0.08 \Omega / \text{phase}$$

$$I_{sc} = 600 \text{ A} \quad V_{oc} (\text{line}) = 900 \text{ V}$$

$$Z_s = \frac{V_{oc} (\text{phase})}{I_a (\text{s.c. phase})} = \frac{\frac{900}{\sqrt{3}}}{600} = \frac{519.33}{600}$$

$$z_s = 0.8655 \text{ M/phase}$$

$$X_s = \sqrt{(Z_s)^2 - (R_a)^2} = \sqrt{(0.8655)^2 - (0.08)^2}$$

$$X_s = \sqrt{0.7490 - 0.0064} = \sqrt{0.7426}$$

$$X_s = 0.86168 \text{ M/phase}$$

$$I_{FL} = \frac{2000 \times 1000}{2300} = 869.56 \text{ A}$$

$$(E_{ph})^2 = (V_{ph} \cos \phi + I_a R_a)^2 + (V_{ph} \sin \phi + I_a X_s)^2$$

$$(E_{ph})^2 = (1342 \times 1 + (869.56 \times 0.08))^2 + (869.56 \times 0.86168)^2$$

$$= (1342 + 69.56)^2 + 561423.56$$

$$(E_{ph})^2 = 3820797.586 + 561423.56$$

$$E_{ph} = \sqrt{2199392.22} \quad E_{ph} = 1483.03 \text{ V}$$

$$\begin{aligned} \% \text{ Regulation} &= \frac{E_{Th} - V_{Th}}{V_{Th}} \times 100 \\ &= \frac{\overbrace{1483.03}^{V_{Th}} - 1342}{1342} \times 100 \\ &= 10.52\% \approx 11\% \end{aligned}$$

For 0.8 p.f laggy

$$\begin{aligned} E_{Th} &= \sqrt{(V_{Th} \cos \phi + I_a R_a)^2 + (V_{Th} \sin \phi + I_a X_s)^2} \\ &= \sqrt{(1342 \times 0.8 + 600 \times 0.08)^2 + (1342 \times 0.6 + 600 \times 0.8616)^2} \\ &= \sqrt{(1073.6 + 48)^2 + (805.2 + 517.08)^2} \\ &= \sqrt{1252986.56 + 1748233.99} \\ &= \sqrt{3006220.55} \\ E_{Th} &= 1733.84 \end{aligned}$$

$$\begin{aligned} \% \text{ Regulation} &= \frac{E_{Th} - V_{Th}}{V_{Th}} \times 100 \\ &= \frac{1733.84 - 1342}{1342} \times 100 \\ &= 29.19\% \end{aligned}$$



8a

Explain the zero power factor method of predetermination of Regulation of an Alternator [08 marks]

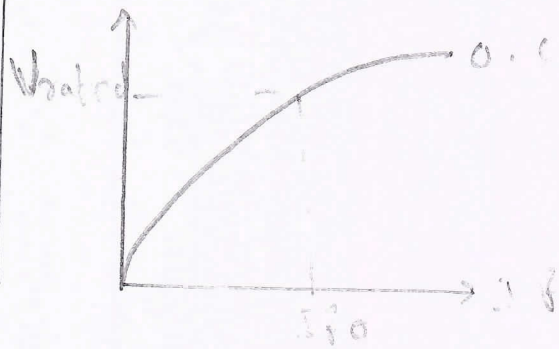
Soln:

Zero Power Factor method is also known as Potier Triangle method.

In this method,  $I_a R_a$  drop and  $I_a X_L$  drop are const quantities but armature reaction is basically const quantity.

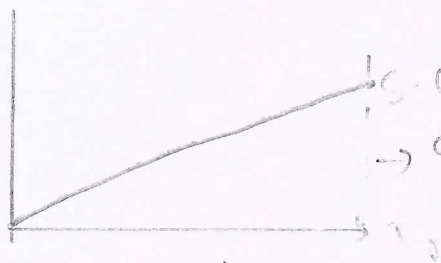
$X_L \Rightarrow$  Potier reactance.

For Z.P.F method, we need O.C test data, S.C test data



$I_{f0}$  is field current required for rated phase voltage on O.C.C curve

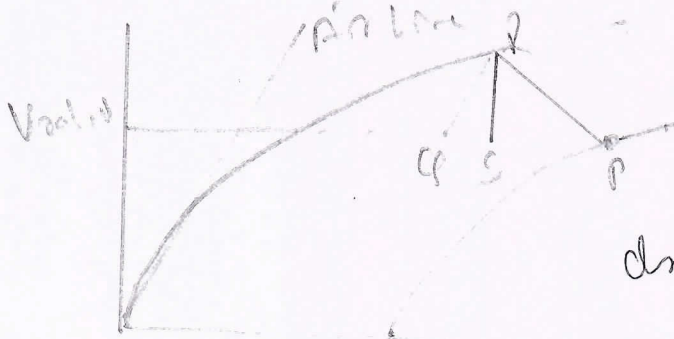
$$X_L = \frac{\text{Scale of } (R_s)}{(I_{a0h}) F.L.}$$



S.C.C curve  
→ Scale of S.C test

Z.P.F test

- 1) Purely inductive load is connected  $\phi = \theta = 90^\circ$
- 2) Alternator is run at synchronous value.
- 3) Excitation is varied till rated full load values are obtained.



Full load Z.P.F Saturation Curve

Scale of  $R_s$  gives voltage drop due to  $X_L$ ,  
 $F_{AR} = \text{Scale of } (R_s)$

8b Compare Synchronous Impedance method and Ampere Turn method of predetermining of voltage Regulation  
[04 marks]

Soln:

1) E on R method

is also called as Synchronous Impedance method

2) Direct load connection not required

3) Indirect method

4) Large  $X_s$ , Higher V.R than Actual  
Pessimistic method

5) O.C Test word  
S.C Test

6) Regulation can be obtained for any load I, P.F

1) on on R method

is also called Ampere Turn method

2) Direct load connection not required

3) Indirect method

4) Lower V.R than Actual  
Optimistic method

5) O.C Test  
S.C Test

6) Regulation at desired power factor can be obtained

8c A 3.5 MW, star connected Alternator at 4160V at 50 Hz has open circuit characteristics

Circuit	50	100	150	200	250	300	350
$I_f$	50	100	150	200	250	300	350
Voc volts line	1629	3150	4160	4750	5130	5320	5550

Field current of 200 A is found necessary in circuit. Full load current on short circuit. Calculate by Ampere turn method Full load V.R at 0.8 p.f lagging. [0.8 mark]

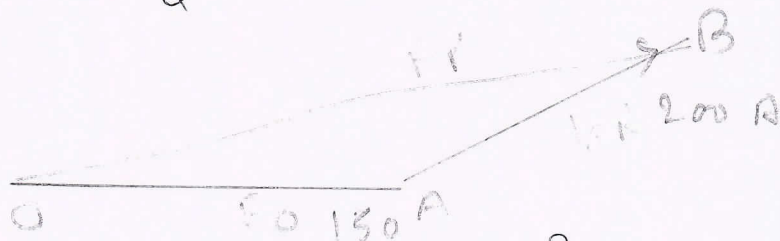
Soln:

Rated Terminal Voltage = 4160V

Field Current =  $I_f = 150 \text{ A} = F_o$

Field current to get Full load current on s.c  $\Rightarrow 200 \text{ A} = F_{AR}$

$$\phi = \cos^{-1}(0.8) = 36.86^\circ$$



$$F_{AR}^2 = F_o^2 + F_{AR}^2 - 2 F_o F_{AR} \cos(90 + \phi)$$

$$= (150)^2 + (200)^2 - 2 \times 150 \times 200 \cos(90 + 36.86)$$

$$F_{AR} = 313.847 \text{ A}$$

From table of Voc line For  $F_{AR} = 313.847$   
the Voc(line) = 5400V (interpolated value)

$$E_{ph} = 5400 \sqrt{3} = 3117.69 \text{ V}$$

$$\% \text{ Regulation} = \frac{3117.69 - 2401.87}{2401.87} \times 100$$

$$= 29.807\%$$

## Module - 5

9  
(a)

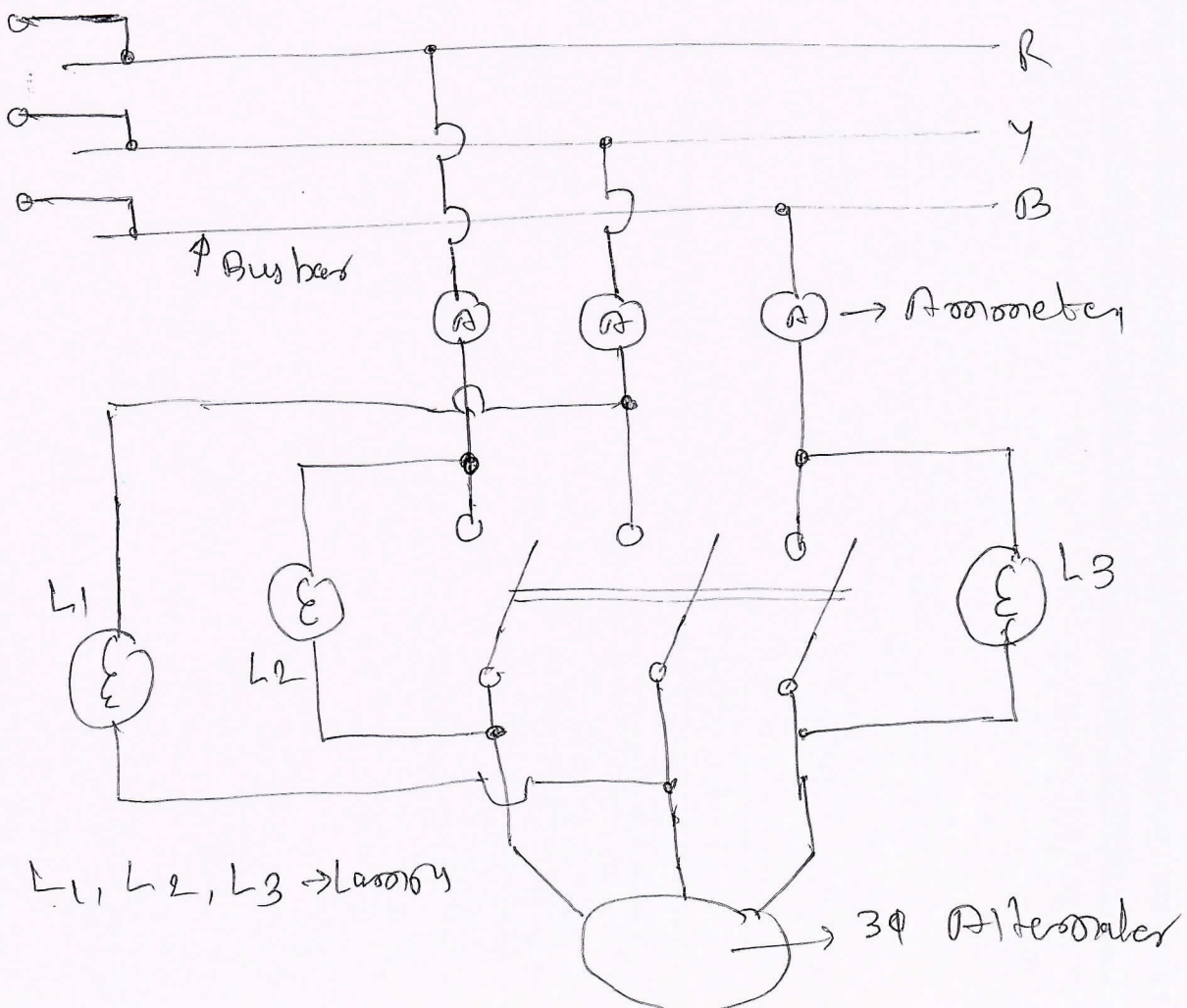
What is Synchronization? Explain with help of neat sketch. The 3 lamp method of synchronization.

[08 marks]

Soln

The process of switching of an alternator to another alternator or with common bus bar without any interruption is called synchronization. The pole synchronized is called as Incoming pole.

- 1) Terminal voltage of incoming pole must be same as that of bus bar voltage and frequency also.
- 2) Phase also should be identical with Bus bar voltage.



For  $V_{\phi}$  Equal frequencies,  $L_1, L_2, L_3$  will flicker at a rate equal to difference in frequency.

For phase sequence correct

All lamps will become dark and bright simultaneously.

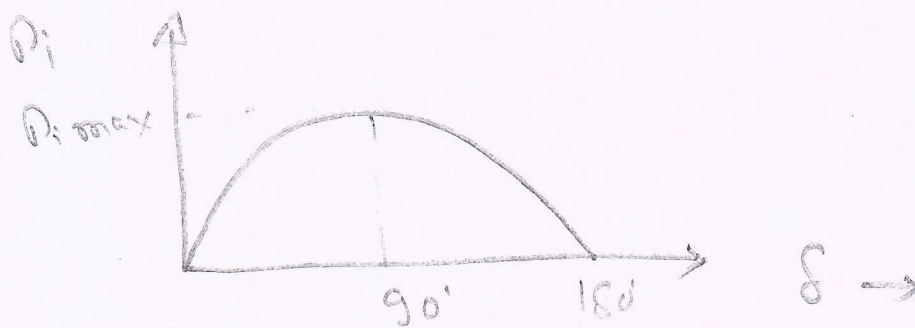
If not done,

Two terminals of incoming side are interchanged.

Correct instant of closing switch is middle of dark period of  $L_1, L_2, L_3$

9  
(b)

Derive an expression for the power angle characteristics of cylindrical rotor alternator. Sketch the Power Angle Curve (OC curve)



$$P = VI \cos \phi \Rightarrow \text{Power o/p per phase}$$

$$P = VI \cos \phi + I^2 R_a \Rightarrow \text{Power i/p}$$

$$\vec{E}^{\wedge} = \vec{V}^{\wedge} + \vec{I}^{\wedge} \vec{Z}_s^{\wedge}$$

$$P_i = \text{mechanical power i/p}$$

$$= \frac{E}{Z_s} [E \cos \delta - V \cos(\delta + \theta)]$$

$$P_o = \frac{-V^2}{Z_s} \cos \theta + \frac{VE}{Z_s} \cos(\delta - \theta)$$

If  $R_a$  is neglected

$$P_o \approx \frac{VE}{Z_s} \sin \delta$$

9c An alternator has a direct axis synchronous reactance of  $0.7 \Omega$  and quadrature axis synchronous reactance of  $0.4 \Omega$ . It is used to supply full load at rated voltage at  $0.8 \text{ p.f.}$ . Find the induced emf on open circuit. (06 marks)

Soln:

$$X_d = 0.7 \Omega$$

$$X_q = 0.4 \Omega$$

$$\cos \phi = \text{p.f.} = 0.8 \quad \text{lag}$$

$$\phi = 36.86^\circ$$

Let Rated Terminal Voltage =  $1 \text{ p.u.}$

Full load Armature Current  $I_a = 1 \text{ p.u.}$

$$R_a = 0$$

$$\tan \psi = \frac{V_t \sin \phi + I_a X_q}{V_t \cos \phi + I_a R_a}$$

$$= \frac{1 \times 0.6 + 1 \times 0.4}{1 \times 0.8 + 1 \times 0}$$

$$= 1.25$$

$$\psi = \tan^{-1}(1.25) = 51.34^\circ$$

$$I_d = I_a \sin \psi = 1 \times \sin 51.34^\circ = 0.7808$$

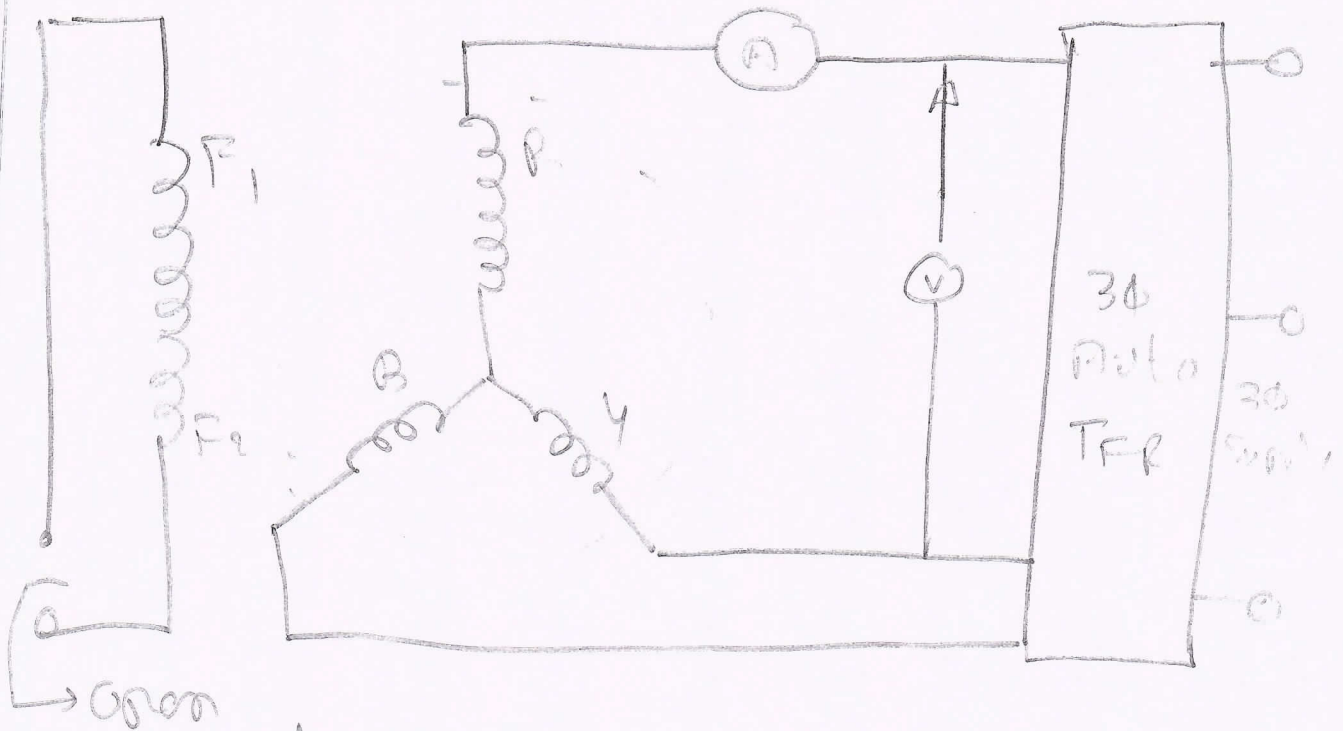
$$E_f = V_t \cos \phi + I_d X_d + I_a R_a$$

$$= 1 \times 0.8 + 0.7808 \times 0.7 + 0$$

$$E_f = 1.5486 \text{ p.u.} = \text{induced emf}$$

## Module 5

- 10  
(a) With help of Circuit Diagram, Explain measurement of direct Axis and Quadrature Axis Reactance by slip Test [08 marks]



Procedure of slip test For  $X_d$  &  $X_q$

- 1) 3 $\phi$  voltage is applied to armature (less than rated voltage)
- 2) Field winding is kept open
- 3) Alternator is run at slightly lesser speed than  $N_s$ .
- 4) Shunt m.m.f aligned with d-axis of field pole then  $\phi_d$  pole is setup. Effective reactance is  $X_d$
- 5) Shunt m.m.f aligned with q-axis  $\phi_q$  pole is set up and effective reactance is  $X_q$

$$X_d = \frac{V_{max}}{I_{min}}$$

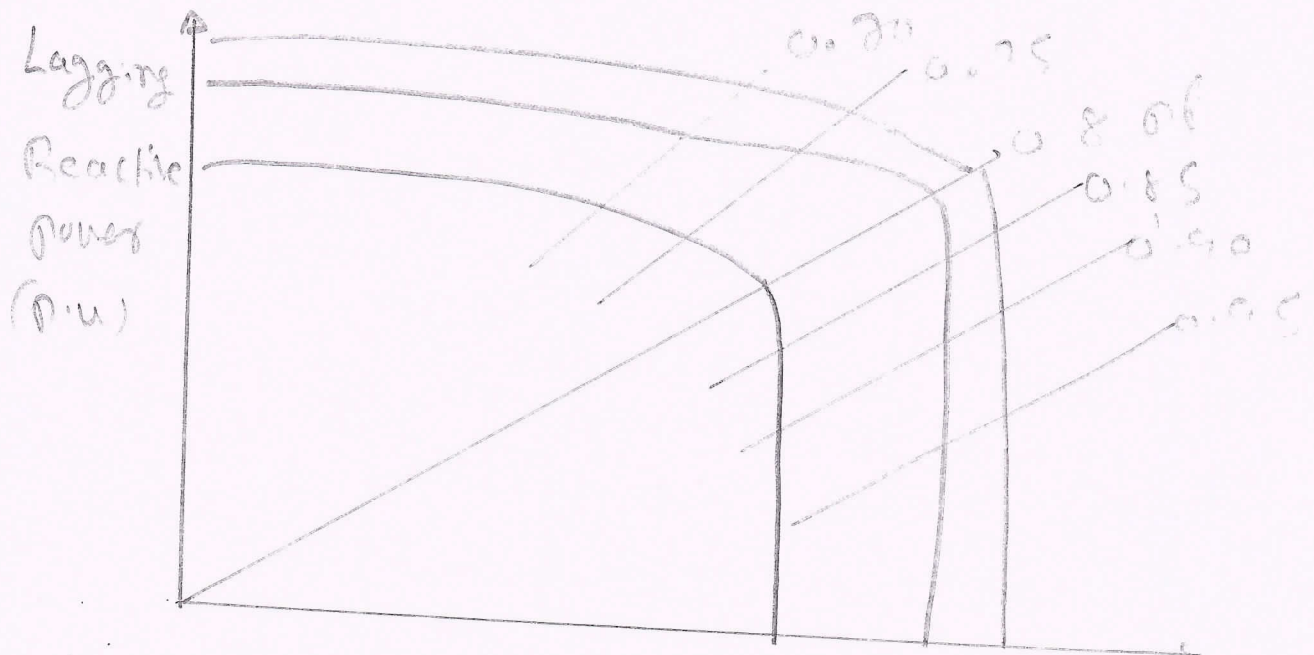
$$X_q = \frac{V_{min}}{I_{max}}$$

10  
(b)

Draw the Capability Curve and  
Explain about the Curve of  
Synchronous Generators

(06 marks)

Soln:



Heating is key factor for Rating of Alternator  
Capability Curve specifies the bounds  
within which machine can operate safely.  
Turbine Rating is the Limiting Factor  
for MW loading.

Operation of Generator, should be away from  
Steady stability limit (of  $90^\circ$ )

Field current also should be within limit.

For unity P.f. or rated P.f.,

Limiting Factor is armature heating

while for P.f. of low value,

field heating is the limiting factor.



10  
c What is Hunting in Synchronous motor?  
How do you eliminate hunting?

(6 marks)

Soln.

Hunting in Synchronous motor (phase swing)

A mechanical phenomenon, where pulsations are produced in voltage, current, and power due to irregular velocity and due to oscillation of rotatory part of motor.

Cause of Hunting

- 1) Sudden change in load
- 2) Change in Frequency
- 3) Sudden change in field current
- 4) A load consists of Harmonic Torques
- 5) A fault in supply system.

Undesirable effects

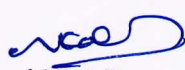
- 1) Severe mechanical stress and large variation in  $I \times \theta$
- 2) Temp rise, Loss in motor
- 3) Unstable machine

Elimination methods of Hunting

- 1) Use of Damper windings - these will damp the oscillation.
- 2) Use of Flywheel
- 3) Design of motor with suitable

for  
(S-on Encoder)

Stiffness Factor.

  
HEAD