

CBCS SCHEME

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BME304

Third Semester B.E./B.Tech. Degree Examination, Dec.2024/Jan.2025 Basic Thermodynamics

Time: 3 hrs.

Max. Marks: 100

- Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.
2. M : Marks , L: Bloom's level , C: Course outcomes.
3. Use of steam table and thermodynamics data hand is permitted.*

Module – 1			M	L	C
Q.1	a.	State and explain zeroth law of thermodynamics.	10	L1	CO1
	b.	Two Celsius thermometers 'A' and 'B' agree at ice point and steam point and the related equation is $t_A = L + Mt_B + Nt_B^2$, where L, M and N are constants, when both thermometer are immersed in fluid, 'A' registers 26°C while 'B' registers 25°C. determine the reading of 'A' when 'B' reads 37.4°C	10	L3	CO1
OR					
Q.2	a.	Derive an expression for work done during : i) Isothermal process ii) Adiabatic process.	10	L2	CO1
	b.	A cylinder contains 1 kg of a certain fluid at an initial pressure of 20 bar. The fluid is allowed to expand reversibly behind a piston according to a law $PV^2 = \text{constant}$ until the volume is doubled. The fluid is then cooled reversibly at constant pressure until the piston regains its original position, heat is then added reversibly with the piston firmly locked in position until the pressure rises to the original value of 20 bar. Calculate the network done by the fluid for an initial volume of 0.05 m ³ and draw a neat PV diagram.	10	L3	CO1
Module – 2					
Q.3	a.	Explain Joule's experiment with sketch.	10	L1	CO2
	b.	Air flows steady at the rate of 0.4 kg/s through an air compressor, entering at 6 m/s with a pressure of 1 bar and a specific volume of 0.85 m ³ /kg and leaving at 4.5 m/s with a pressure of 6.9 bar and a specific volume of 0.16 m ³ /kg. The internal energy of the air leaving is 88 kJ/kg greater than that of the air entering. Cooling water in a jacket surrounding the cylinder absorbs heat from the air at the rate of 59 W. Calculate the power required to drive the compressor and the inlet and outlet cross-sectional areas.	10	L3	CO2
OR					
Q.4	a.	Derive Steady Flow Energy Equation (SFEE) with a neat sketch.	10	L2	CO2
	b.	A turbine operates in a steady flow conditions, receiving steam at the following state : pressure 1.2 MPa, temperature 188°C, enthalpy 2785 kJ/kg, velocity 34 m/s, and elevation 3 m. The steam leaves the turbine at the following state : pressure 20 KPa, enthalpy 2512 kJ/kg, velocity 100 m/s and elevation 0 m. Heat is lost to the surroundings at the rate of 0.29 kJ/s. If the rate of the steam flow through the turbine is 0.42 kg/s. What is the power output of the turbine in KW?	10	L3	CO2
Module – 3					
Q.5	a.	State and explain Kelvin - Plank and clausius statements of II law of thermodynamics.	10	L2	CO3
	b.	A heat engine receives half of its heat at 1000 K and the rest at 500 K while rejecting heat to a sink at 300 K. What is the maximum possible efficiency of this heat engine?	10	L3	CO3

OR

Q.6	a.	State and prove clausius inequality.	10	L1	CO3
	b.	A heat engine working on a Carnot cycle absorbs heat from three thermal reservoirs at 1000 K 800 K and 600 K respectively. The engine does 10 KW of net work and rejects 400 kJ/min of heat to the sink at 800 K, if heat supplied by the reservoir at 1000 K 60% heat supplied by reservoir at 600 K. Find the quantifier of heat supplied by each reservoir.	10	L3	CO3

Module – 4

Q.7	a.	Explain the concept of available and unavailable energy referred to a cycle.	10	L1	CO4
	b.	In a steam generator, water evaporated at 260°C, while the combustion gas ($C_p = 1.08 \text{ kJ/kg K}$) is cooled from 1300°C to 320°C. The surrounding are at 30°C. Determine loss in energy available due to the above heat transfer per kg of water evaporated (Latent heat of vaporization of water at 260°C = 1662.5 $\text{m}^3 \text{ kgmole}$).	10	L3	CO4

OR

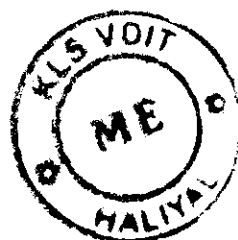
Q.8	a.	Sketch and explain throttling calorimeter.	10	L2	CO4
	b.	A vessel of 0.04 m^3 contains a mixing of saturated water and saturated steam at temperature of 240°C. The mass of the liquid is 8 kg. Find the pressure, specific volume, enthalpy, entropy and internal energy.	10	L3	CO4

Module – 5

Q.9	a.	Explain : i) Vander Waal's equation of state ii) Compressibility factor iii) Law of corresponding states.	10	L2	CO5
	b.	1 kg of CO_2 has a volume of 0.86 m^3 at 120°C compute pressure using : i) Ideal gas equation ii) Vander Waal's equation. Take Vander Waal's constants for CO_2 $a = 365.6 \text{ KNM}^4/\text{kg mole}$ and $b = 0.0423 \text{ m}^3/\text{kg mole}$.	10	L3	CO5

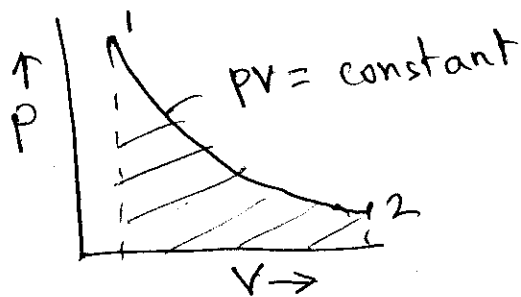
OR

Q.10	a.	Discuss Maxwell's equations and Tds equation.	10	L2	CO5
	b.	Volumetric analysis of a gaseous mixture yields the following results : $\text{CO}_2 = 12\%$, $\text{O}_2 = 4\%$, $\text{N}_2 = 82\%$, $\text{CO} = 2\%$. Determine the analysis on mass basis, molecular weight and gas constant for the mixture, assume ideal gas behavior.	10	L3	CO5



Q.No.	Solution and Scheme	Marks
1. a	<p>The Zeroth law of thermodynamics states that if two systems are each in thermal equilibrium with a third system, then they are also in thermal equilibrium with each other.</p> <p>This law establishes a concept of temperature and thermal equilibrium, implying that objects at the same temperature will not exchange heat when brought into contact.</p> <p>Imagine three systems A, B and C. If system 'A' is in thermal equilibrium with system C, and system 'B' is also in thermal equilibrium with system C, then according to zeroth law of thermodynamics, system 'A' and system 'B' are also in thermal equilibrium with each other.</p>	2 4
	<pre> graph TD A[A] -- q=0 --> B[B] A[A] -- q=0 --> C[C] B[B] -- q=0 --> C[C] </pre>	
b.	$L=0$ at ice point	2
	$M + 100N = 1, N = \frac{1}{1875}$	2
	$M = \frac{1975}{1875} = 1.0533$	2
	$t_A = 38.6^\circ\text{C}$ at $t_B = 37.4^\circ\text{C}$	4

2 a. (i) Isothermal Process



$$W = \int_1^2 P \, dV \quad \text{--- --- --- ①}$$

$$PV = \text{constant}$$

$$P_1 V_1 = P_2 V_2 = PV$$

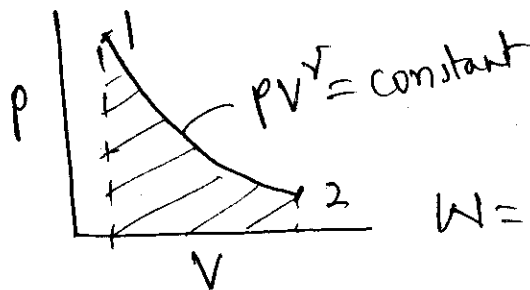
$$P = \frac{P_1 V_1}{V}$$

Substituting in Eq ①

$$W = \int_1^2 P_1 V_1 \frac{dV}{V}$$

$$= P_1 V_1 \ln\left(\frac{V_2}{V_1}\right) = P_2 V_2 \ln\left(\frac{V_2}{V_1}\right) \quad \text{--- 4}$$

(ii) Adiabatic Process



$$P_1 V_1^\gamma = P_2 V_2^\gamma = PV^\gamma \quad \text{--- 2}$$

$$P = \frac{P_1 V_1^\gamma}{V^\gamma} = P_1 V_1^\gamma V^{-\gamma}$$

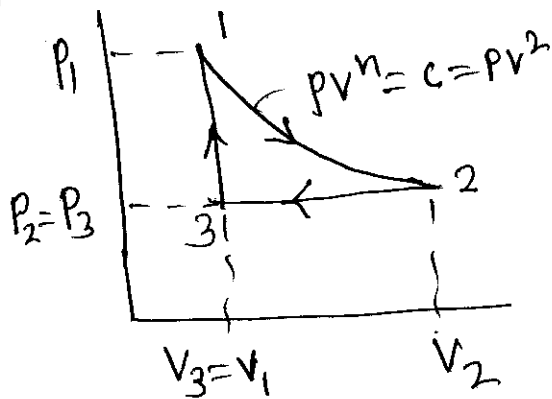
$$W = \int_1^2 P_1 V_1^\gamma V^{-\gamma} \, dV \quad \text{--- --- 2}$$

$$= P_1 V_1^\gamma \left(\frac{V_2^{-\gamma+1}}{-\gamma+1} - \frac{V_1^{-\gamma+1}}{-\gamma+1} \right) \quad \text{--- 2}$$

$$= \frac{P_2 V_2 - P_1 V_1}{1-\gamma}$$

$$= \frac{P_1 V_1 - P_2 V_2}{\gamma-1} \quad \text{--- --- 2}$$

2 b.



$$P_1 = 20 \text{ bar}$$

$$m = 1 \text{ kg}$$

$$n = 2$$

$$V_2 = 2V_1 = 0.1 \text{ m}^3$$

$$V_1 = 0.05 \text{ m}^3$$

$$P_2 = 5 \text{ bar.}$$

$$W_{1-2} = \frac{P_1 V_1 - P_2 V_2}{n-1} = 50 \text{ KJ}$$

Process 2-3

$$W_{2-3} = P(V_3 - V_2) = -25 \text{ KJ}$$

(Work done on the system)

Process 3-1

$$W_{3-1} = 0 \text{ (constant volume process)}$$

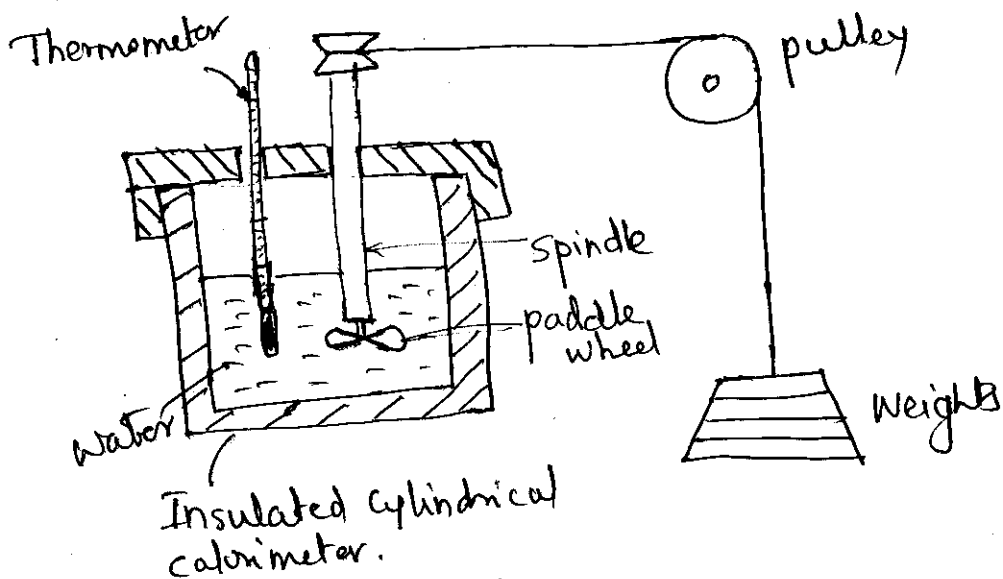
Net work done

$$W_{\text{net}} = W_{1-2} + W_{2-3} + W_{3-1}$$

$$= 50 - 25 + 0 = 25 \text{ KJ}$$

3a. Joule's experiment demonstrated the mechanical equivalent of heat, showing that mechanical work can be converted into heat energy and vice versa.

The experiment involved a system with paddle wheel immersed in water, where the potential energy of falling weights was converted into the kinetic energy of the paddle wheel, which in turn increases the water's temperature.



paddle wheel is made to rotate by raising and lowering of weight, pulley rotates during this. As the paddle wheel rotates, the intermolecular collision takes place between water molecules causing temperature of the water to raise, Kinetic energy of water molecules increases.

After repeated experiments, Joule calculated the work done and proportional heat generated. Then the relation between mechanical work and heat was established which is

$$W = J \cdot Q$$

$$W = 4.186 Q$$

3b. $m = 0.4 \text{ kg/s}$, $u_1 = 6 \text{ m/s}$, $P_1 = 1 \text{ bar}$, $v_1 = 0.85 \text{ m}^3/\text{kg}$
 $u_2 = 4.5 \text{ m/s}$, $P_2 = 6.9 \text{ bar}$, $v_2 = 0.16 \text{ m}^3/\text{kg}$.
 $u_2 = 88 \text{ kJ/kg} + u_1$, $Q = 59 \text{ W}$. $A_1 = ?$, $A_2 = ?$, $W = ?$
 SFEE

$$m \left(u_1 + P_1 v_1 + \frac{v_1^2}{2} + z_1 \right) + Q$$

$$= m \left(u_2 + P_2 v_2 + \frac{v_2^2}{2} + z_2 \right) + W$$

$$\begin{aligned}
 W &= m \left[(u_1 - u_2) + (p_1 v_1 - p_2 v_2) + \frac{v_1^2 - v_2^2}{2} + z_1 - z_2 \right] + Q \\
 &= 0.4 \left[-88 + (100 \times 0.85 - 6.9 \times 10^2 \times 0.16) + \frac{6^2 - 4.5^2}{2} \times 10^{-3} \right. \\
 &\quad \left. + 0 \right] + 59 \times 10^{-3} \\
 &= -45.416 \text{ kW}
 \end{aligned}$$

4

$$m = 0.4 = \frac{A_1 v_1}{v_1} = \frac{A_2 v_2}{v_2}$$

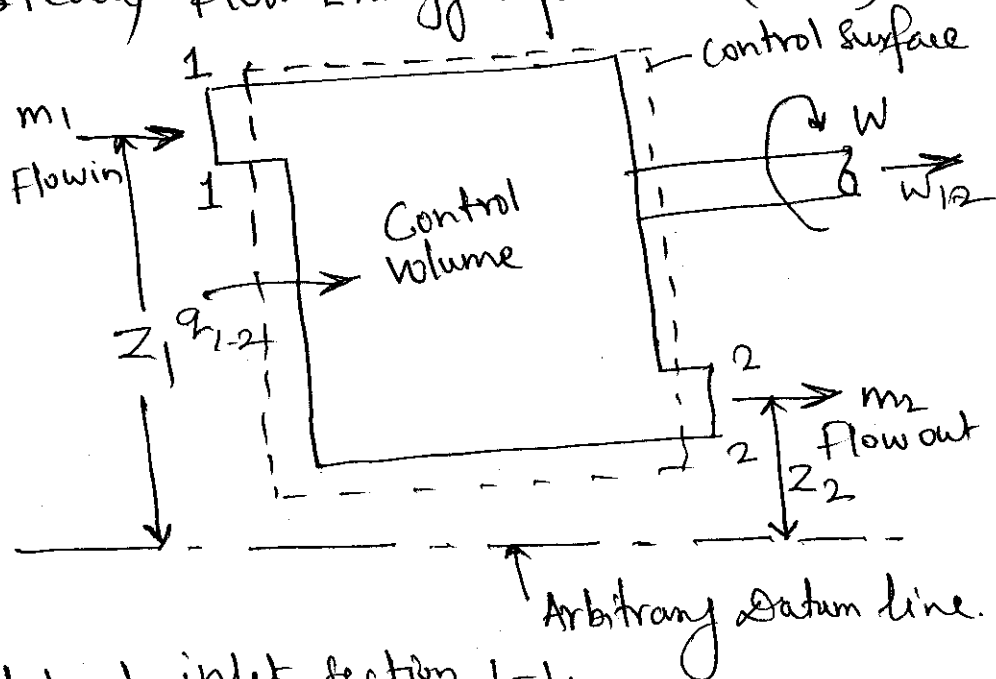
$$A_1 = \frac{m v_1}{v_1} = \frac{0.4 \times 0.85}{6} = 0.0567 \text{ m}^2$$

2

$$A_2 = \frac{m v_2}{v_2} = \frac{0.4 \times 0.16}{4.5} = 0.0142 \text{ m}^2$$

2

4 a. Steady Flow Energy Equation (SFEE)



4

Let at inlet section 1-1.

p_1 = pressure of working fluid (N/m^2)

v_1 = Sp. volume (m^3/kg)

V_1 = velocity of working fluid

u_1 = Sp. internal energy (KJ/kg)

z_1 = height above datum line (m)

1117 at outlet section 2-2

P_2, v_2, V_2, u_2, z_2 be the corresponding values of working fluid leaving control volume

q_{1-2} be the heat supplied to control volume (kJ/kg)

w_{1-2} be the work done by the system (kJ/kg)

Considering 1 kg of mass of working fluid, $m = 1$ kg

Energy entering the control volume is

$e_1 = \text{Internal energy} + \text{Displacement work} + \text{KE} + \text{PE} + \text{Heat supplied}$

$$e_1 = u_1 + P_1 v_1 + \frac{V_1^2}{2} + g z_1 + q_{1-2} \quad (\text{kJ/kg})$$

Total energy leaving the control volume,

$$e_2 = u_2 + P_2 v_2 + \frac{V_2^2}{2} + g z_2 + w_{1-2}$$

Total energy entering = Total energy leaving

$$e_1 = e_2$$

$$u_1 + P_1 v_1 + \frac{V_1^2}{2} + g z_1 + q_{1-2} = u_2 + P_2 v_2 + \frac{V_2^2}{2} + g z_2 + w_{1-2} \quad 4$$

$$h_1 + \frac{V_1^2}{2} + g z_1 + q_{1-2} = h_2 + \frac{V_2^2}{2} + g z_2 + w_{1-2}$$

Above equation is called SFEE

4b.

$$P_1 = 1.2 \times 10^3 \text{ kN/m}^2, T_1 = 188^\circ\text{C}, h_1 = 2785 \text{ kJ/kg}$$

$$V_1 = 34 \text{ m/s}, z_1 = 3 \text{ m}$$

$$P_2 = 20 \text{ kN/m}^2, h_2 = 2512 \text{ kJ/kg}, V_2 = 100 \text{ m/s}, z_2 = 0$$

$$Q = -0.29 \text{ kJ/s}, m = 0.42 \text{ kg/s}, w_{1-2} = ?$$

SFEE

$$m \left(h_1 + \frac{V_1^2}{2} + g z_1 \right) + Q = m \left(h_2 + \frac{V_2^2}{2} + g z_2 \right) + W$$

$$0.42 \left(2785 + \frac{34^2}{2} \times 10^{-3} + 9.81 \times 3 \times 10^3 \right) - 0.29$$

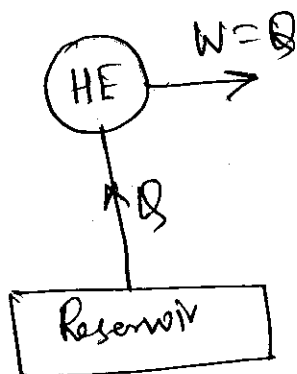
$$= 0.42 \left(2512 + \frac{100^2}{2} \times 10^{-3} + 9.81 \times 0 \times 10^3 \right) + W$$

W = 112.515 KW.

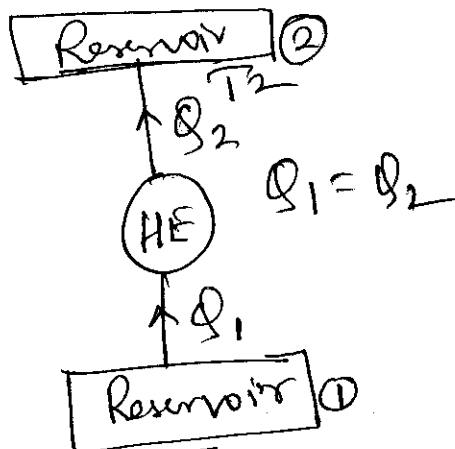
5 a, Kelvin-Planck statement states that it is impossible to construct an engine working in reversible cycle whose sole effect is transferring heat from reservoir and converting it into equivalent amount of work. It implies that 100% efficient machine is not possible, it puts restriction on energy conversion limits.

Clausius statement states it is impossible to transfer heat from lower temperature to higher temperature without the aid of external power supply.

It puts restriction on direction of flow of energy.



Violation of Kelvin-Planck Statement



Violation of Clausius Statement

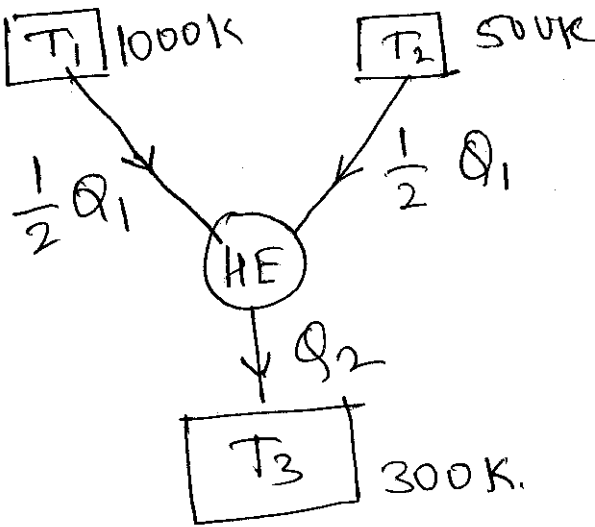
Above figures represents the violation of both statements

4

4

2

5 b.



2

$$\frac{\frac{1}{2} Q_1}{T_1} + \frac{\frac{1}{2} Q_2}{T_2} - \frac{Q_2}{300} = 0$$

2

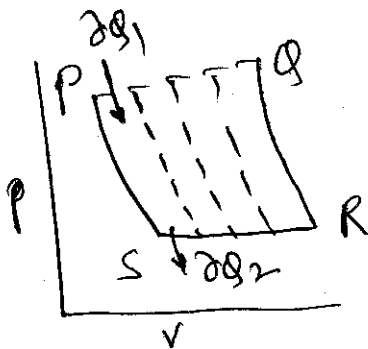
$$Q_2 = 0.45 Q_1$$

$$\eta = \frac{-Q_2 + Q_1}{Q_1} = \frac{Q_1 - 0.45 Q_1}{Q_1} = 55\%$$

2

4

6 a.



Consider cycle PQRS in which PQ is irreversible or irreversible process, other processes QR, RS, SP are reversible processes.

Dividing this cycle into large number of smaller cycle & considering any one of such cycles say 1-2-3-4, the thermal efficiency is

$$\eta = 1 - \left(\frac{\delta Q_2}{\delta Q_1} \right) = 1 - \frac{T_2}{T_1}$$

For irreversible process cyclic integration of $\frac{\delta Q}{T}$ will never become zero. $\oint \frac{dQ}{T} \neq 0$.

$$\eta_{irr} \leq \eta_{rev}$$

$$1 - \left(\frac{\delta Q_2}{\delta Q_1} \right)_{irr} \leq 1 - \left(\frac{\delta Q_2}{\delta Q_1} \right)_{rev}$$

$$\left(\frac{\delta Q_2}{\delta Q_1}\right)_{irr} \geq \left(\frac{\delta Q_2}{\delta Q_1}\right)_{rev}$$

$$\frac{\delta Q_2}{\delta Q_1} \geq \frac{T_2}{T_1}$$

$$\frac{\delta Q_2}{T_2} \geq \frac{\delta Q_1}{T_1}$$

$$\therefore \frac{\delta Q_1}{T_1} - \frac{\delta Q_2}{T_2} \leq 0$$

$$\frac{\delta Q_1}{T_1} - \left(-\frac{\delta Q_2}{T_2}\right) \leq 0 \quad (\because \delta Q_2 \text{ is } -ve)$$

$$\therefore \frac{\delta Q_1}{T_1} + \frac{\delta Q_2}{T_2} \leq 0$$

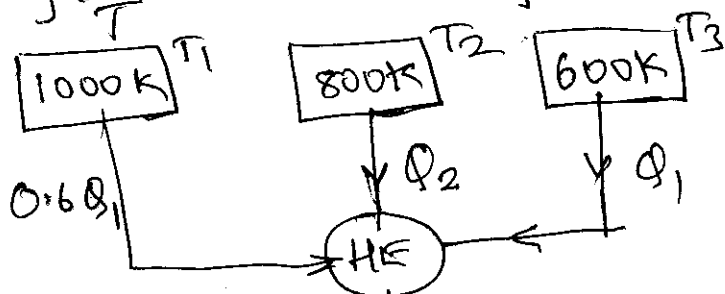
$\oint \frac{\delta Q}{T} \leq 0$ is Clausius inequality

$\oint \frac{\delta Q}{T} = 0$ For reversible cycle

$\oint \frac{\delta Q}{T} < 0$ For irreversible cycle.

$\oint \frac{\delta Q}{T} > 0$ For impossible cycle.

6b.



$$Q_2 = 400 \text{ kJ/min}$$

$$W = 10 \text{ kW} = 600 \text{ kJ/min}$$

$$0.6Q_1 - Q_2 + Q_1 = W = 600$$

$$1.6Q_1 - 400 = 600$$

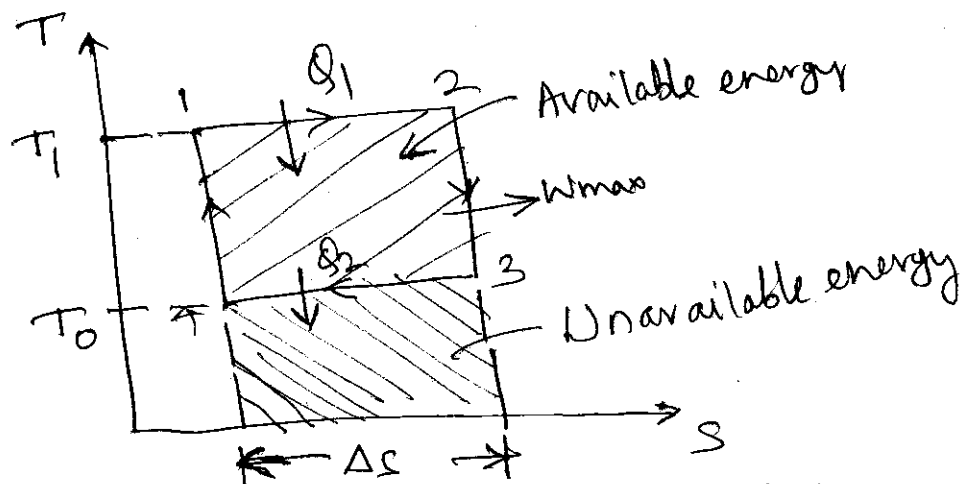
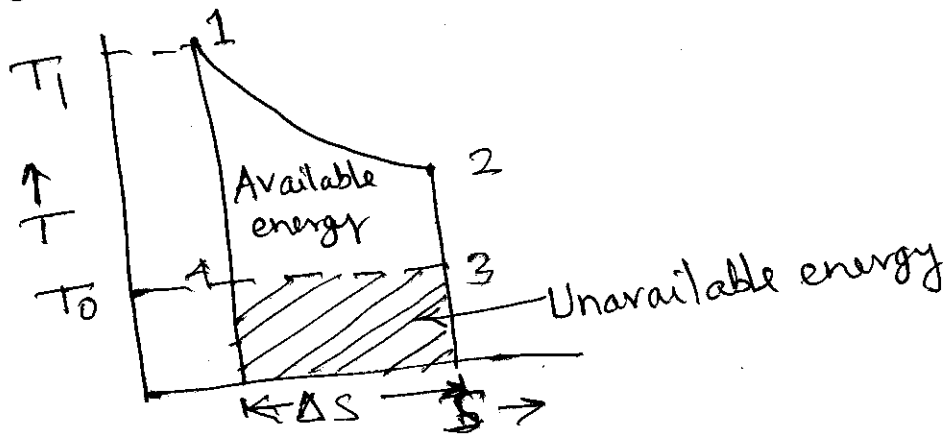
$$Q_1 = 625 \text{ kJ/min}$$

$$\dot{Q}_2 = 400 \text{ kJ/min}$$

7a. The available energy or availability of a given system is defined as the maximum useful work that can be obtained in a process until a system reaches equilibrium with surroundings or dead state. It can be completely converted into useful work.

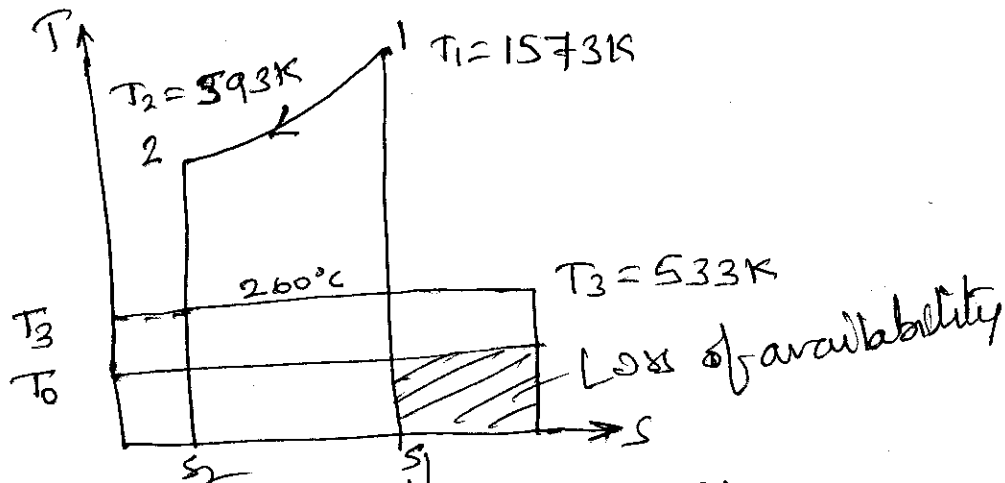
The unavailable energy is the other part of energy which cannot be converted into useful work.

The available and unavailable energy for a closed system undergoing cyclic process is shown below



$$\begin{aligned} \text{Available energy} &= \text{Heat supplied} - \text{Unavailable energy} \\ &= \underline{Q_1 - T_0 \Delta s} \end{aligned}$$

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$$C_p \text{ of gas} = 1.08 \text{ kJ/kgK}, T_0 = 303 \text{ K},$$

$$h_{fg} = 1662.5 \text{ kJ/kg}$$

$$AE_{\text{gas}} = h_1 - h_2 - T_0 (s_1 - s_2)$$

$$= m_g (T_1 - T_2) - T_0 \ln(T_1/T_2)$$

$$= m_g \times 1.08 [(1573 - 593)] - 303 \ln(1573/593)$$

$$= m_g \times 739.16 \text{ kJ}$$

$$AE_{\text{water}} = (T_3 - T_0) m_w h_{fg} / T_3$$

$$= (533 - 303) \times 1662.5 / 533$$

$$= m_w \times 717.4 \text{ kJ} \quad (m_w = 1 \text{ kg})$$

$$m_g c_p (T_2 - T_1) = m_w h_{fg}$$

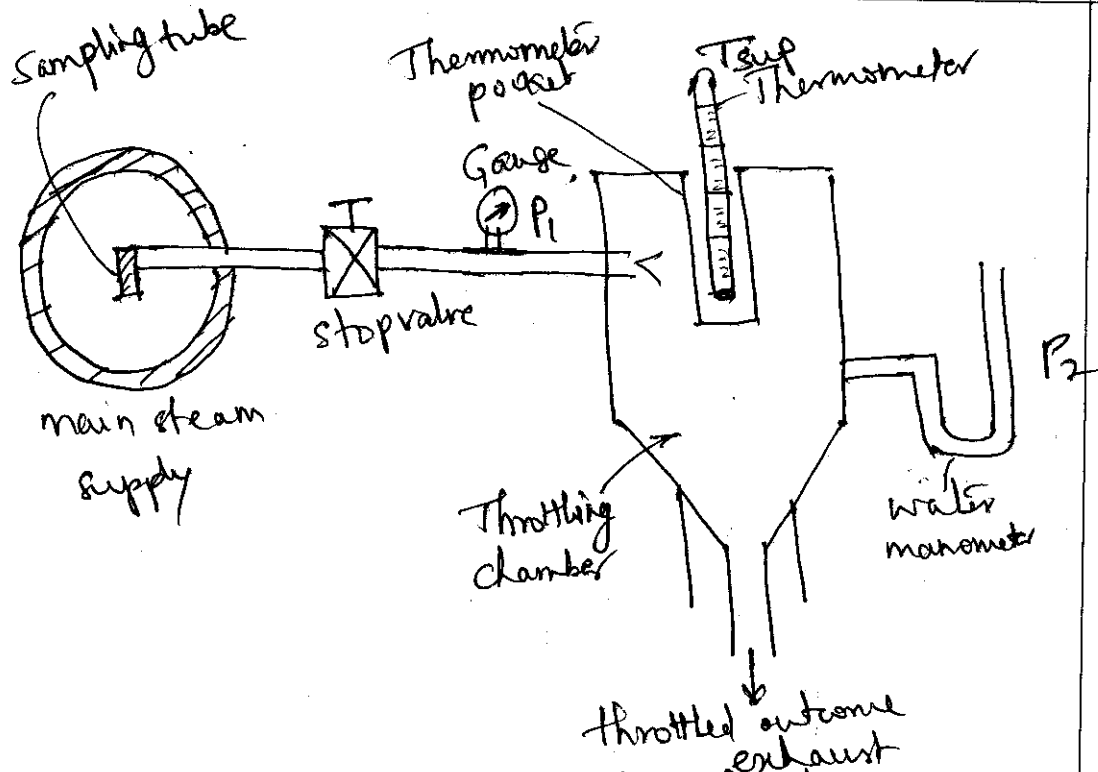
$$AE_{\text{gas}} = 1161.1 \text{ kJ}$$

$$\text{Loss of availability} = AE_{\text{gas}} - A_w$$

$$= 1161.1 - 717.4$$

$$= 443.7 \text{ kJ}$$

8a



Throttling calorimeter is used when the steam is dry. First stop valve is opened fully so that the steam is not partially throttled as it passes through the apparatus for a while to allow pressure and temperature to stabilise. If the pressure is very close to atmospheric, the saturation should be around 100°C , it may be assumed that the steam is superheated. When the steady condition is reached, gauge pressure is noted. After throttling, the temperature and pressure from thermometer and manometer are recorded. The barometric pressure is also recorded.

$$h_1 = h_2$$

$$h_{\text{wat}} P_1 = h_{\text{sup}} \text{ at } P_2$$


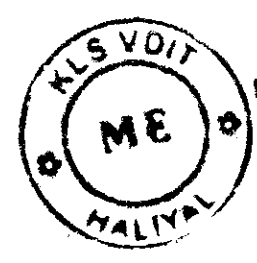

$$h_{f1} + x h_{fg1} = h_{g2} + c_p (T_{\text{sup}} - T_{\text{sat}})$$

$$\text{Dryness fraction, } x = \frac{h_{g2} + c_p (T_{\text{sup}} - T_{\text{sat}}) - h_{f1}}{h_{fg1}}$$

Q.No.	Solution and Scheme	Marks
8.b	<p>Volume of vessel, $= 0.04 \text{ m}^3$</p> <p>$T_{\text{sat}} = 240^\circ\text{C}$</p> <p>Mass of liquid $= m_l = 8 \text{ kg} = \text{liquid mass}$</p> <p>from steam table, at $T_{\text{sat}} = 240^\circ\text{C}$</p> <p>$P = 33 \text{ bar}$, $h_f = 1034 \text{ kJ/kg}$, $h_{fg} = 1770 \text{ kJ/kg}$</p> <p>$v_g = 0.0605 \text{ m}^3/\text{kg}$, $v_f = 0.001229 \text{ m}^3/\text{kg}$</p> <p>$h_g = 2802 \text{ kJ/kg}$, $s_f = 2.703 \text{ kJ/kgK}$, $s_{fg} = 3.439 \text{ kJ/kgK}$</p> <p>$s_g = 6.141 \text{ kJ/kgK}$.</p> <p>Total volume of liquid occupied</p> <p>$V_l = m_l \times v_f = 8 \times 0.001229 = 0.009792 \text{ m}^3$ 2</p> <p>Total volume occupied by steam (V_s)</p> <p>$V = V_l + V_s$</p> <p>$0.04 = 0.009792 + V_s$ 2</p> <p>$V_s = 0.030208 \text{ m}^3$</p> <p>Mass of steam ($m_s$)</p> <p>$m_s = \frac{V_s}{v_g} = \frac{0.030208}{0.0605} = 0.499 \text{ kg}$ 2</p> <p>Mass of liquid and steam, $m = m_l + m_s$</p> <p>$= 8 + 0.499$</p> <p>$= 8.499 \text{ kg}$ 2</p> <p>Total sp. volume of the mixture</p> <p>$v = \frac{V}{m} = \frac{0.04}{8.499} = 0.0047 \text{ m}^3/\text{kg}$</p> <p>$v = v_f + x v_{fg}$</p> <p>$0.0047 = 0.001229 + x(0.0605 - 0.001229)$</p> <p>$x = 0.058 \approx 0.06$</p> <p>$h = h_f + x h_{fg} = 1034 + 0.058 \times 1770 = 1141 \text{ kJ/kg}$</p> <p>$S = s_f + x s_{fg} = 2.703 + 0.058(3.439) = 2.9 \text{ kJ/kg}$</p>	<p>2</p> <p>2</p> <p>2</p> <p>2</p>

Q.No.	Solution and Scheme	Marks
	<p>Internal Energy</p> $u = h - Pv = 1141.5 - 33 \times 100 \times 0.0047$ $u = 1125.99 \text{ KJ/Kg.}$	
9 a.	<p>(i) Vander waals Equation.</p> <p>It is a modification in ideal gas equation to take into account molecular size and molecular interaction forces.</p> $\left[P + a \left(\frac{n}{V} \right)^2 \right] \left[\frac{V}{n} - b \right] = RT$ <p>The constants a, b are characteristic of individual gas.</p>	3
	<p>(ii) Compressibility Factor:</p> <p>Real gases deviate from ideal gas behaviour. This deviation at given temperature and pressure can be accurately accounted by introduction of correction factor called compressibility factor, Z.</p> $Z = \frac{Pv}{RT} \quad \text{or} \quad Pv = ZRT$ $Z = \frac{V_{\text{act}}}{V_{\text{ideal}}}, \quad \text{for ideal gas, } Z = 1$	3
	<p>(iii) Law of corresponding states: An additional assumption about real gases made by Vander waals was that all gases at corresponding states should behave similarly.</p> <p>The corresponding state that Vander waals choose to use is called reduced state, which is based on derivation of conditions of a substance from its own critical condition.</p> $P_R = P/P_c, \quad V_R = V/V_c, \quad T_R = T/T_c$ <p>Vander waals equation becomes</p> $\left(P_R + \frac{3}{V_R^2} \right) \left(V_R - \frac{1}{3} \right) = \frac{8}{3} T_R$ <p>Critical parameter of gas can be expressed in terms of a and b parameters.</p> $V_c = 3b, \quad P_c = \frac{a}{27b^2}, \quad T_c = \frac{8a}{27bR}$	4

Q.No.	Solution and Scheme	Marks
9. b.	<p>(i) Using ideal gas equation</p> $R = \frac{\bar{R}}{M} = 188.95 \text{ Nm/kg-K}$ $Pv = mRT$ $P = \frac{mRT}{v} = 86.345 \text{ kPa}$ <p>(ii) Using vander Waals equation</p> $\left(P + \frac{a}{v^2}\right)(\bar{v} - b) = \bar{R}T$ $\bar{v} = v \times M/m = 37.84 \text{ m}^3/\text{kg m}$ $P = \frac{RT}{\bar{v} - b} - \frac{a}{\bar{v}^2} = 86.44 \text{ kPa}$	<p>2</p> <p>2</p> <p>2</p> <p>4</p>
10a.	<p>a) $du = Tds - Pdv$</p> <p>b) $dH = du + PdV + Vdp = Tds + vdp$</p> <p>c) $dF = du - Tds - sdt = -Pdv - sdt$</p> <p>d) $dG = dH - Tds - sdt = vdp - sdt$</p> <p>Simplifying</p> $\left(\frac{\partial T}{\partial v}\right)_s = -\left(\frac{\partial P}{\partial s}\right)_v, \left(\frac{\partial T}{\partial P}\right)_s = \left(\frac{\partial v}{\partial s}\right)_v$ $\left(\frac{\partial P}{\partial T}\right)_v = \left(\frac{\partial s}{\partial v}\right)_T, \left(\frac{\partial v}{\partial T}\right)_P = -\left(\frac{\partial s}{\partial P}\right)_T$ <p>Tds equations</p> $T\left(\frac{\partial s}{\partial T}\right)_P = C_p \quad \& \quad \left(\frac{\partial s}{\partial P}\right)_T = -\left(\frac{\partial v}{\partial T}\right)_P$ $Tds = C_p dT - T\left(\frac{\partial v}{\partial T}\right)_P dP$	<p>4</p> <p>4</p> <p>4</p> <p>2</p>
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Q.No.	Solution and Scheme	Marks										
10.b.	<p>Molecular weight of mixture</p> $\sum X_{im} = 30.08$ <table border="0"> <tr> <td>Content</td> <td>Mass fraction</td> </tr> <tr> <td>CO₂</td> <td>0.1755</td> </tr> <tr> <td>O₂</td> <td>0.0425</td> </tr> <tr> <td>N₂</td> <td>0.764</td> </tr> <tr> <td>CO</td> <td>0.0186</td> </tr> </table> <p>Gas constant of Mixture</p> $R_{mixture} = \frac{\bar{R}}{\sum X_M} = 0.276 \text{ kJ/kg K.}$ <div style="display: flex; justify-content: space-between; align-items: flex-start;"> <div style="text-align: center;">  <p>Dr. S.V. Channopattana Professor Mechanical Engg. Dept. KLS VJIT Haliyal</p> </div> <div style="text-align: center;">  </div> <div style="text-align: center;">  <p>HOD Mechanical Engineering KLS Vishwanathrao Deshpande Institute of Technology Haliyal-581329</p> </div> </div>	Content	Mass fraction	CO ₂	0.1755	O ₂	0.0425	N ₂	0.764	CO	0.0186	
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